MATHEMATICAL EXPLANATION TO SOLUTION FOR EX-NOR PROBLEM USING MLFFN

Vaibhav Kant Singh
Department of Computer Science and Engineering, Institute of Technology, Guru Ghasidas Vishwavidyalaya, Central University, Bilaspur, Chhattisgarh, India

ABSTRACT

This paper is in continuation to what we did previously in the field of Soft Computing. In the previous work the author proposed several solutions to the XOR problem. In this paper we will see some solutions to the Ex-NOR problem using the concept of MLFFN. Ex-NOR problem is a non-linearly separable problem the solutions of which are discussed in this paper. The Artificial Neural Network proposed is mathematically proved to be successful in providing solution to the Ex-NOR problem. The solutions proposed are explained by means of Architectural Graph and Signal flow graph.

KEYWORDS

Artificial Neural Network, Ex-NOR, Activation function, Signal Flow Graph & Architectural Graph

1. INTRODUCTION

Soft Computing is the branch of Computer Science that deals with methodologies that solve the problems which portray imprecision, partial truth and uncertainty. In Soft Computing the impression is tolerable. Computational time when compared with Hard Computing is less due to the presence of intelligent computational steps. Soft Computing involves systems which are basically inspired from nature like Artificial Neural Network and Fuzzy Logic. The programs made are going to follow new laws which are going to justify the logic behind the programming done. The output produced need not to be deterministic in nature. It may allow parallel computation. It is capable to produce approximate result to the problem posed by the user. Soft Computing is basically a branch that deals with three known streams for the implementation of the idea that it portrays. The three streams are Artificial Neural Network, Fuzzy Systems and Genetic Algorithm and Evolutionary Programming.

In this paper the author Vaibhav Kant Singh focuses on the stream Artificial Neural Network. Artificial Neural Network (ANN) is a stream that deals with construction of systems which are having analogy in working with the Biological Neural Network working. The ANN systems are capable of mapping input to output. ANN systems are capable to get trained; they are capable to learn from previous examples. ANN is capable of generalization. ANN having resemblance with Biological Network of Neurons are robust and fault tolerant in nature. Some currently existing ANN systems are Adaptive Resonance Theory (ART), Bidirectional Associative Memory (BAM), Perceptron (Single Layer and Multilayer), ADALINE and MADALINE, Counter Propagation Network, Multi Layer Feed Forward Network (MLFFN), Hopfield Network,

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Artificial Neural Network systems comprises of three basic elements namely the Individual neurons present in the ANN, the network topology (the network architecture) and the learning algorithm employed to train the ANN.

2. LITERATURE SURVEY


3. PROBLEM STATEMENT

The Ex-NOR problem is non-linearly separable problem. The Definition of linear separability is two sets of points A and B in an n-dimensional space are called linearly separable if (n+1) real numbers \( w_1, w_2, \ldots, w(n+1) \) exists, such that every point \((x_1, x_2, \ldots, x_n) \in A\) satisfies \( wi x i = 1 \geq w(n+1) \) exist and every point \((x_1, x_2, \ldots, x_n) \in B\) satisfies \( wi x i = 1 < w(n+1) \) exist. Table 1 represents the Ex-NOR logic and the Figure in Table 1 specifies the portrayal of the inputs applicable for Ex-NOR problem in Two-dimensional plane. It is very clear from the table that it is not possible to divide the inputs into two classes on the basis of output. Thus from the research that the author Vaibhav Kant Singh [1,2,5] made earlier the problem is a non-linearly separable problem.
4. PROPOSED SOLUTIONS

In this paper we will see some solutions to the Ex-NOR problem using MLFFN.

4.1. First Proposed Solution to the Ex-NOR problem

In first proposed solution a MLFFN is proposed which comprises of three layers. The First layer comprises of two neurons. The second layer comprises of one neuron. The third layer comprises of one neuron. The first layer comprises of non-linear neuron. The second and third layer comprises of neurons which are having linear in nature. The neurons are characterized linear and non-linear on the basis of the characteristic they exhibit. The naming of the network could be (2-2-1-1). The solution proposed specifies the final values for weights acquired after training the network. After attaining the values prescribed in the solution the proposed ANN gives the desired values for output for the applicable input to the Ex-NOR logic GATE. In this section we will see the mathematical proof of the provided solution. Figure 1 represents the proposed Architectural Graph for the problem, whereas the Figure 2 represents the Signal Flow Graph giving the detail of the weights and other parameters involved in the ANN. In the Architectural graph NL represents nonlinear whereas LE represents Linear element. Z represents the output produced by the ANN.

Figure 1: Architectural Graph representing First and Third Solution to Ex-NOR Problem
Here, the activation function used for non linear elements in the hidden layer is hyperbolic tangent function. Definition of hyperbolic tangent function is:
\[
\tan h x = \frac{\sinh x}{\cosh x} = \frac{e^x - e^{-x}}{e^x + e^{-x}} = \frac{e^{2x} - 1}{e^{2x} + 1} = \frac{1 - e^{-2x}}{1 + e^{-2x}} \ldots (5)
\]

Here, \( e = 2.7182818456 \) i.e. the natural logarithm base known as Euler’s number, \( x \) = induced local field value and Range of values for function will be \([-1, +1]\). At node3 the signal value will be (From Eq(2) & Eq(5))
\[
\Psi(-1.5) = \frac{1 - e^{-2x(-1.5)}}{1 + e^{-2x(-1.5)}} = \frac{-19.08553692}{21.08553692} = (-0.905148253) \ldots \ldots \ldots \ldots \ldots (6)
\]

At node4 the signal value will be (From Eq(4) & Eq(5))
\[
\Psi(-0.5) = \frac{1 - e^{-2x(-0.5)}}{1 + e^{-2x(-0.5)}} = \frac{-1.718281828}{3.718281828} = (-0.462117157) \ldots \ldots \ldots \ldots \ldots (7)
\]

At node5 the signal value will be (From Eq(6) & Eq(7))
node5 = node3 \times -1 + node4 \times 1 + 1 \times (-0.5) \ldots \ldots (8)
node5 = (-0.9051482253) \times (-1) + (-0.462117157) \times 1 - 0.5 = (-0.056968904) \ldots (9)
The value produced by node5 in Eq(9) will be squashed by the linear activation function i.e. the threshold function. Since, in the output layer the neuron present exhibits linear characteristics in minimum configuration MLFFN. Definition of Threshold function is :-

\[
\Psi(x) = \begin{cases} 
0, & x < \text{threshold} \\
1, & x \geq \text{threshold} 
\end{cases} \quad \cdots \cdots \cdots \cdots (10)
\]

Here, threshold=0. From Eq(9) and Eq(10) the value of y when x1=0 and x2=0 will be 
\[y = \Psi(-0.056968904) = 0 \quad \cdots \cdots (11)\]
Since \((-0.056968904 < 0)\)

\[
\epsilon(x) = \begin{cases} 
0, & x < \text{threshold} \\
1, & x \geq \text{threshold} 
\end{cases} \quad \cdots \cdots \cdots \cdots (12) \quad [\text{threshold}=0 \text{ for Eq}(12) ]
\]

From Eq. (11) the value of node6 will be 
\[\text{node6} = y \times -1 + 1 \times 0 \quad \cdots \cdots (13)\]
Therefore, here 
\[\text{node6} = 0 \times -1 + 1 \times 0 = 0 \quad \cdots \cdots (14)\]

From, (12) and (14) the value of output z for input x1=0 and x2=0 will be 1,
\[z = \epsilon(0) = 1 \quad \cdots \cdots \cdots \cdots (15)\]
Since \((0 = 0)\)

CASE2:- [x1=1 and x2=0 ]
At node1 the signal value will be from Eq(1) = 1 + 0 - 1.5 = (-0.5) \cdots \cdots \cdots \cdots (16)
At node2 the signal value will be from Eq(3) = 1 + 0 - 0.5 = 0.5 \cdots \cdots \cdots \cdots \cdots \cdots \cdots (17)
At node3 the signal value will be from Eq(16) & Eq(5)
\[ \text{node}3 = \psi(-0.5) = \frac{1 - e^{-2 \times (-0.5)}}{1 + e^{-2 \times (-0.5)}} = \frac{-1.718281828}{3.718281828} = (-0.462117157) \ldots \ldots (18) \]

At node4 the signal value will be from Eq(17) & Eq(5)
\[ \text{node}4 = \psi(0.5) = \frac{1 - e^{-2 \times (0.5)}}{1 + e^{-2 \times (0.5)}} = \frac{0.632120558}{1.367879441} = (0.462117156) \ldots \ldots (19) \]

At node5 the signal will be from Eq(18), Eq(19) & Eq(8)
\[ \text{node}5 = (-0.462117157) \times -1 + (0.462117156) \times 1 - 0.5 \times 1 = (0.424234313) \ldots (20) \]

Therefore the value of y for x1=1 and x2=0 from Eq(20) and Eq(10) is
\[ y = \psi(0.424234313) = 1 \ldots (21) \text{Since } 0.424234313 > 0 \]

From Eq(14) the value of node6 will be node6 = 1 \times -1 + 0 \times 1 = -1 \ldots (22)
From Eq(12) and Eq(22) the output z for the input x1=1 and x2=0 will be 0
\[ z = \epsilon(-1) = 0 \ldots \ldots \ldots \ldots \ldots (23) \text{Since } (-1 < 0) \]

**CASE 3:** [x1=0 and x2=1]
At node1 the signal value will be from Eq(1)= 0 + 1 - 1.5 = (-0.5) \ldots (24)
At node2 the signal value will be from Eq(3)= 0 + 1 - 0.5 = (0.5) \ldots (25)

At node3 the signal value will be from Eq(24) & Eq(5)
\[ \psi(-0.5) = \frac{1 - e^{-2 \times (-0.5)}}{1 + e^{-2 \times (-0.5)}} = \frac{-1.718281828}{3.718281828} = (-0.462117157) \ldots (26) \]
At node 4 the signal value will be from Eq(25) & Eq(5)
\[ \Psi(0.5) = \frac{1 - e^{-2 \times 0.5}}{1 + e^{-2 \times 0.5}} = \frac{0.632120558}{1.367879441} = 0.46217156 \] ................ (27)

At node 5 the signal value will be from Eq(26), Eq(27) & Eq(8)=
\((-0.462117157 \times -1) + (0.462117156 \times 1) - 0.5 \times 1 = (0.424234313) \) ................ (28)

Therefore the value of y for x1=0 and x2=1 from Eq(22) and Eq(10) is
\[ y = \Psi(0.424234313) = 1 ............. (29) \text{ Since } (0.424234313 > 0) \]

From Eq(14) the value of node 6 will be node 6 = 1 \times -1 + 0 \times 1 = -1 ........ (30)
From Eq(12) and Eq(30) the output z for the input x1=0 and x2=1 will be 0
\[ z = \epsilon(-1) = 0 ............... (31) \text{ Since } (-1 < 0) \]

**CASE 4:-** [x1=1 and x2=1]
At node 1 the signal value will be from Eq(1) = (1 + 1 - 1.5) = (0.5) ........ (32)
At node 2 the signal value will be from Eq(3) = (1 + 1 - 0.5) = (1.5) ............ (33)

At node 3 the signal value will be from Eq(32) & Eq(5)
\[ \Psi(0.5) = \frac{1 - e^{-2 \times 0.5}}{1 + e^{-2 \times 0.5}} = \frac{0.632120558}{1.367879441} = (0.462117156) \] ................ (34)

At node 4 the signal value will be from Eq(33) and Eq(5)
\[ node 4 = \Psi(1.5) = \frac{1 - e^{-2 \times 1.5}}{1 + e^{-2 \times 1.5}} = \frac{0.950212931}{1.049787068} = 0.905148253 \] ................ (35)

At node 5 the signal value will be from Eq(34), Eq(35) and Eq(8)=
\( (0.462117156 \times -1) + (0.905148253 \times 1) - 0.5 = (-0.056968902) \) ........ (36)

Therefore, the value of y when x1=1 and x2=1 will be from Eq(36) and Eq(10)
\[ y = \Psi(-0.056968902) = 0 ........ (37) \text{ Since } (-0.056968902 < 0) \]

From Eq(14) the value of node 6 will be node 6 = 0 \times -1 + 0 \times 1 = 0 ........ (38)
From Eq(12) and Eq(38) the output z for the input x1=1 and x2=1 will be 0
\[ z = \epsilon(0) = 1 ........ (39) \text{ Since } (0 = 0) \]

From Equations Eq(15), Eq(23), Eq(31) and Eq(39) the first solution provided is proved to be a valid solution.
4.2. Second Proposed Solution to the Ex-NOR problem

In this section we will see the second proposed solution to the Ex-NOR problem. The proposed solution is a MLFFN comprising of three layers. Each layer comprises of one neuron each. The first layer comprises of one neuron. The neuron in layer one is non-linear. The neuron in layer two and three are linear in nature. Figure 3 and Figure 4 represent Architectural Graph and Signal Flow Graph for the proposed solution.
Figure 4. Signal flow graph representing the second solution to the Ex-NOR problem using MLFFN.
In this case for output neuron which is linear element we will be using threshold function as the activation function. The threshold value is 1.35. The definition of Threshold function is:-
In this case for output neuron which is linear element we will be using threshold function as the activation function. The threshold value is 1.35. The definition of Threshold function is:

\[ \psi(x) = \begin{cases} 1 & \text{if } x \geq \text{threshold} \\ 0 & \text{if } x < \text{threshold} \end{cases} \quad (g) \]

Here, \( x \) = induced local field value. From Eq.(f) and Eq.(g) we get the value of \( y \) for \( x_1=0 \) and \( x_2=0 \) as

\[ y = \psi(1.310296508) = 0 \quad \text{.........(h)Since (1.310296508 < 1.35)} \]

\[ \epsilon(x) = \begin{cases} 0, & x < \text{threshold} \\ 1, & x \geq \text{threshold} \end{cases} \quad \text{.........(i) [ threshold=0 for Eq(i) ]} \]

From Eq. (h) the value of node4 will be node4 = \( y \times -1 + 1 \times 0 \) .... (j)

Therefore, here node6 = \( 0 \times -1 + 1 \times 0 = 0 \) .... (k)

From, (i) and (k) the value of output \( z \) for input \( x_1=0 \) and \( x_2=0 \) will be 1,

\[ z = \epsilon(0) = 1 \quad \text{.................(l) Since (0 = 0)} \]

CASE 2:-

\( x_1=1 \) and \( x_2=0 \)

At node1 value of the signal will be from Eq(a) = \( 1 + 0 - 1.5 = (-0.5) \) .......... (m)
At node 2 value of the signal will be from Eq(n) & Eq(c)
\[\text{node 2} = \psi(-0.5) = \frac{1 - e^{-2 \times (-0.5)}}{1 + e^{-2 \times (-0.5)}} = \frac{-1.718281828}{3.718281828} = (-0.462117157) \quad \ldots \ldots \ldots \quad (n)\]

At node 3 value of the signal will be from Eq(n) & Eq(e)
\[\text{node 3} = 1 + 0 + (-2 \times -0.462117157) - 0.5 = (1.424234314) \quad \ldots \ldots \ldots \quad (o)\]

The value of y for x1=1 and x2=0 will be from Eq(o) & Eq(g)
\[y = \psi(1.424234314) = 1 \quad \ldots \ldots \quad (p) \quad \text{Since} \quad (1.424234314 > 1.35)\]

From Eq(j) the value of node 4 will be node 4 = 1 \times -1 + 0 \times 1 = -1 \quad \ldots \ldots \quad (q)

From Eq(i) and Eq(q) the output z for the input x1=1 and x2=0 will be 0
\[z = \varepsilon(-1) = 0 \quad \ldots \ldots \ldots \ldots \quad (r) \quad \text{Since} \quad (-1 < 0)\]

CASE 3: [x1=0 and x2=1]
At node 1 the value of signal from Eq(n) = (0 + 1 - 1.5) = (-0.5) \quad \ldots \ldots \ldots \quad (s)
At node 2 the value of signal from Eq(s) & Eq(c)
\[\text{node 2} = \psi(-0.5) = \frac{1 - e^{-2 \times (-0.5)}}{1 + e^{-2 \times (-0.5)}} = \frac{-1.718281828}{3.718281828} = (-0.462117157) \quad \ldots \ldots \ldots \quad (t)\]

At node 3 the value of the signal from Eq(t) and Eq(e)
\[\text{node 3} = (0 + 1 + (-2 \times -0.462117157) - 0.5 = (1.424234314) \quad \ldots \ldots \ldots \quad (u)\]

Therefore the value of y for the input x1=0 and x2=1 will be from Eq(u) and Eq(g)
\[y = \psi(1.424234314) = 1 \quad \ldots \ldots \quad (v) \quad \text{Since} \quad (1.424234314 > 1.35)\]

From Eq(j) the value of node 6 will be node 6 = 1 \times -1 + 0 \times 1 = -1 \quad \ldots \ldots \quad (w)
From Eq(i) and Eq(w) the output z for the input x1=0 and x2=1 will be 0

From Equations Eq(l), Eq(r), Eq(x) and Eq(D) the first solution provided is proved to be a valid solution.
4.3. Third Proposed Solution to the Ex-NOR problem

In Third proposed solution a MLFFN is proposed which comprises of three layers. The First layer comprises of two neurons. The second layer comprises of one neuron. The third layer comprises of one neuron. The first layer comprises of non-linear neuron. The second and third layer comprises of neurons which are having linear in nature. The neurons are characterized linear and non-linear on the basis of the characteristic they exhibit. The naming of the network could be (2-2-1-1). The solution proposed specifies the final values for weights acquired after training the network. After attaining the values prescribed in the solution the proposed ANN gives the desired values for output for the applicable input to the Ex-NOR logic GATE. In this section we will see the mathematical proof of the provided solution. Figure 1 represents the proposed Architectural Graph for the problem, whereas the Figure 5 represents the Signal Flow Graph giving the detail of the weights and other parameters involved in the ANN. In the Architectural graph NL represents nonlinear whereas LE represents Linear element. Z represents the output produced by the ANN.
**CASE 1:** When \( x_1=0 \) and \( x_2=0 \),

At node 1 value of signal will be 
\[
x_1 \times x_2 = (0 \times 1) + (0 \times x_2) = 0 + 0 \times (-0.5) = (-0.5)
\]

\( (1a) \)

At node 2 Signal value will be 
\[
x_1 \times -1 + x_2 \times 1 + x_1 \times (-0.5) = (0 \times -1) + (0 \times 1) + (0 \times (-0.5)) = (-0.5)
\]

\( (2a) \)

At node 3 Signal value will be 
\[
x_1 \times x_2 + x_1 \times (-0.5) = (0 \times 0) + (0 \times (-0.5)) = (-0.5)
\]

\( (3a) \)

At node 4 Signal value will be 
\[
x_1 \times x_2 + x_2 \times (-0.5) = (0 \times x_2) + (0 \times (-0.5)) = (-0.5)
\]

\( (4a) \)

Here, the activation function used for hidden layer is Hyperbolic tangent function. The Def. of which is given below:

\[
\tanh x = \frac{\sinh x}{\cosh x} = \frac{(e^x - e^{-x})}{(e^x + e^{-x})} = \frac{(e^{-2x} - 1)}{(e^{-2x} + 1)} = \frac{(1 - e^{-2x})}{(1 + e^{-2x})} \quad \text{here } e = 2.718281828456...
\]

\( (5a) \)

\( x \) = induced local field value, \( e \) = The natural logarithm base also known as Euler’s number & Range=[-1,+1]

At node 3 the signal value will be from Eq 2 and 5
\[
\Psi(-0.5) = \frac{(1 - e^{-2x-0.5})}{(1 + e^{-2x+0.5})} = \frac{-1.718281828}{3.718281828} = (-0.462117157)
\]

\( (6a) \)

At node 4 the signal value will be from Eq 4 and 5
\[
\Psi(-0.5) = \frac{(1 - e^{-2x-0.5})}{(1 + e^{-2x-0.5})} = \frac{-1.718281828}{3.718281828} = (-0.462117157)
\]

\( (7a) \)

At node 5 the signal value will be from Eq 6 and Eq 7

\[
\text{node} 3 \times 1 + \text{node} 4 \times 1 + x \times (-0.5) = (-0.462117157) \times 1 + (-0.462117157) \times 1 + 1 \times (-0.5) = (-1.424234314)
\]

\( (8a) \)

In the output layer the function used is Threshold function. The Definition of the threshold function is given below:

\[
\Psi(x) = \begin{cases} 
1 & \text{if } x \geq \text{threshold} \\
0 & \text{if } x < \text{threshold}
\end{cases} \quad \text{here threshold value is set to value } -1 
\]

\( (10a) \)

\[
y = \Psi(-1.424234314) = 0 \quad \text{Since, } ((-1.424234314) < -1) 
\]

\( (11a) \)

\[
\epsilon(x) = \begin{cases} 
0, & x < \text{threshold} \\
1, & x \geq \text{threshold}
\end{cases} \quad \text{[threshold=0 for Eq(12a)]}
\]

\( (12a) \)
CASE 2:- When x₁=1 and x₂=0,
At node 1 value of signal will be x₁ × 1 + x₂ × −1 + 1 × (−0.5)
Substituting the value of x₁ and x₂ = 1 × 1 + 0 × −1 + 1 × (−0.5) = (0.5) ........(16a)

At node 2 Signal value will be x₁ × −1 + x₂ × 1 + 1 × (−0.5),
Substituting the value of x₁ and x₂ = 1 × −1 + 0 × 1 + 1 × (−0.5) = (−1.5) .... (17a)

At node 3 the signal value will be from Eq(16a and 5a)
Ψ(0.5) = \frac{(1 - e^{−2×0.5})}{(1 + e^{−2×0.5})} = \frac{0.632120558}{1.367879441} = (0.462117156) ................. (18a)

At node 4 the signal value will be from Eq (17a and 5a)
Ψ(−1.5) = \frac{(1 - e^{−2×−1.5})}{(1 + e^{−2×−1.5})} = \frac{−19.08553692}{21.08553693} = (−0.905148253) ................. (19a)
At node 5 the signal value will be from Eq 18a, Eq. 19a and Eq 8a
= (0.462117156) × 1 + (−0.905148253) × 1 + 1 × (−0.5) = (−0.943031097) .... (20a)

From Eq(20a) and Eq(10a) the value of y for the second case i.e. x₁=1 and x₂=0 will be
Ψ(−0.943031097) = 1 Since, (−0.943031097) > −1) ................. (21a)

From Eq(14a) the value of node6 will be node6 = 1 × −1 + 0 × 1 = −1 .... (22a)
From Eq(12a) and Eq(22a) the output z for the input x₁=1 and x₂=0 will be 0
\[ z = \varepsilon(-1) = 0 \quad \ldots \quad (23a) \text{ Since } (-1 < 0) \]

**CASE 3:** When \( x_1 = 0 \) and \( x_2 = 1 \),
At node 1 value of signal will be \( x_1 \times 1 + x_2 \times -1 + 1 \times (-0.5) \)
Substituting the value of \( x_1 \) and \( x_2 \)
\[ = 0 \times 1 + 1 \times -1 + 1 \times (-0.5) = (-1.5) \ldots (24a) \]
At node 2 signal value will be \( x_1 \times -1 + x_2 \times 1 + 1 \times (-0.5) \)
Substituting the value of \( x_1 \) and \( x_2 \)
\[ = 0 \times -1 + 1 \times 1 + 1 \times (-0.5) = (0.5) \ldots (25a) \]

At node 3 the signal value will be from Eq(24a and 5a)
\[ \Psi(-1.5) = \frac{(1 - e^{-2 \times -1.5})}{(1 + e^{-2 \times -1.5})} = \frac{-19.08553692}{21.08553693} = (-0.905148253) \ldots \ldots \ldots (26a) \]

At node 4 the signal value will be from Eq (25a and 5a)
\[ \Psi(0.5) = \frac{(1 - e^{-2 \times 0.5})}{(1 + e^{-2 \times 0.5})} = \frac{0.632120558}{1.367879441} = (0.462117156) \ldots \ldots \ldots \ldots (27a) \]

At node 5 the signal value will be from Eq 26a, Eq 27a and Eq 8a
\[ = (-0.905148253) \times 1 + (0.462117156) \times 1 + 1 \times (-0.5) = (-0.943031097) \ldots (28a) \]

From Eq(28a) and Eq(10a) the value of \( y \) for the third case i.e. \( x_1 = 0 \) and \( x_2 = 1 \) will be
\[ y = \Psi(-0.943031097) = 1 \text{ Since, } ((-0.943031097) > -1) \ldots \ldots \ldots (29a) \]
3. CONCLUSIONS

In this paper two solutions to the Ex-NOR problem is proposed using the MLFFN. From the proposed solutions it is clear that it is possible to solve non-linearly separable problem using Multilayer Network. All the proposed solutions comprises of three layers where the elements in the network may be of either type i.e. Non-linear or Linear. The mathematical proof satisfies the condition for Ex-NOR.
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Author

Vaibhav Kant Singh, [LM ISTE] and [LM CSI] is currently working as Assistant Professor in the Department of Computer Science & Engineering, Institute of Technology, Guru Ghasidas Vishwavidyalaya, (Central University), Bilaspur, (C.G.), India. He is having around Eight years of teaching experience. He is having papers published in both international and national conferences. His papers are published in national and international journals too. His Papers are published by Publishers like Springer, ACM, AIP, WASET, Recently one paper Accepted for Publication in Elsevier, One paper accepted in first round for publication in IEEE Explore etc. In International Conferences papers are published in Conferences organized by IIT’s, IIIT’s, CSI, WASET etc. He has taught several subjects like, AI and Expert System, Data Mining, Soft Computing (ANN, Genetic Algorithm and Fuzzy Logic), Network Programming, Compiler Design, Advanced Programming through JAVA, OOP through C++, Prolog, Lisp, Internet Fundamentals and Application, Parallel Computing, Operating System,DAA etc.