ROBUST OPTIMIZATION FOR RCPSP UNDER UNCERTAINTY

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ABSTRACT

The aim of the present article is to optimize the robustness objective for the Resource-Constrained Project scheduling Problem (RCPSP) dealing with activity duration uncertainty. The studied robustness consists in minimizing the worst-case performance, referred to as the min-max robustness objective, among a set of initial scenarios. We propose an enhanced GRASP approach as a solution to the given scenario-based robust model. This approach is based on different priority rules in the construction phase and a forward-backward heuristic in the improvement phase. We investigate two different benchmark data sets, the Patterson set and the PSPLIB J30 set. Experiments show that the proposed enhanced GRASP outperforms the basic procedure, and a based-evolutionary algorithm, in robustness optimization.

KEYWORDS

RCPSP, uncertainty, Robust optimization, GRASP, FBI

1. INTRODUCTION

Deterministic Resource-Constrained Project Scheduling Problem (RCPSP) is a well-known project scheduling problem that consists in scheduling a set of activities over resources with limited capacities subject to precedence and resource constraints while optimizing several objectives. The most common objective is to minimize the project duration (so called makespan and denoted by C_{max}). The RCPSP is classified as an NP-hard problem [1], and tackled with various approaches in the literature.

However, during execution, projects are subject to unexpected disruptions caused by different ways such that activities may take longer than their estimated durations, new activities may be inserted or retreated, resources may be broken down, which causes delays, and project spend more time than its initial expected duration. Thus, many researchers 'reflects, on project scheduling, are concentrated in managing uncertainty during the scheduling process by establishing new scheduling approaches such that robust approaches. The goal of a robust approach is to generate one or more robust schedules with the guarantee of performance whenever disturbances occurred. Consequently, the schedule robustness is the capability to absorb unexpected system variability with the minimum cost.

Although heuristic and metaheuristics are still suitable way to resolve complex problems, they are less investigated when dealing with uncertainty. From this point of view, we are encouraged to apply an enhanced GRASP approach to the RCPSP under uncertainty. Based on scenarios, the studied robust optimization problem aims to minimize the min-max robustness objective. The proposed approach is combined with a forward-backward improvement heuristic.

The next section points out the most of works related on scheduling under uncertainty from the literature, especially for RCPSP. Section 3 focuses on the problem definition in deterministic and non deterministic version. Section 4 describes, in general, the main phases of the GRASP method.

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In section 5, we present the application of the latter method to the robust RCPSP. Computational results are given in section 6. Section 7 concludes this article.

2. LITERATURE REVIEW

Deterministic RCPSP was widely studied in the literature. Heuristics and metaheuristics were successfully applied in this context, such as Genetic Algorithms, Sampling methods, based local search methods, Simulated Annealing, etc. Efficient surveys are given in the following references [2, 3]. As described, the RCPSP have been the research subject of an important amount of literature.

However, during execution, projects are subject to disruption due to initial uncertain data, a lack of information, or unexpected dynamic events. Recently, authors have investigated efficient efforts on scheduling problems dealing with uncertainty. In [4], the authors have classified approaches dealing with uncertainty in two main axes: reactive approaches and proactive approaches. The first class concerns approaches which react on-line, during schedule execution; they are usually based on scheduling policies (scheduling strategy). Thus, a dynamic schedule may be modified during their execution; we distinguish the purely reactive procedures, also called dynamic approaches, and the predictive-reactive approaches which are based on an initial predictive schedule. Proactive approaches (called robust approaches) work off-line and do not change the schedule is permitted during execution. Thus, they consider in advance, before the beginning of the schedule the probable parameters changes that could occur on-line and generate schedules with the guarantee of a performance level. More details about approaches designed for project scheduling are presented by Horroelen and Leus [5].

A robust optimization aims to find a solution having the best worst-case performance across a finite or infinite set of scenarios [6]. A scenario represents a problem realization founded by matching fixed values to uncertain problem parameters. The scenario-based approach, inspired from the decision analysis, is an efficient way to model uncertainty inspired from the decision analysis. A robust schedule is defined as the schedule which guarantees a good performance for all possible scenarios, and remains with highest performance for all scenarios. Schedule robustness is evaluated in terms of mean value, worst-case, worst-case deviation, etc [7]. Two well known robustness objectives are studied in the literature: the absolute robustness, and the absolute regret robustness, referred to as, the *min-max* robustness, and the *min-max regret* robustness, respectively. With the absolute robustness objective, the aim is to minimize the maximum performance degradation among all scenarios. However, the min-max regret robustness objective is to minimize the maximum deviation of solutions from optimality across all scenarios. In the literature [8], Kouvelis and Yu have investigated the cited robustness objectives for different combinatorial optimization problems.

Although robust scheduling problems take into consideration uncertainty in different real-life cases, solution methods for robust RCPSP are not exhaustive. In [9], Al Fawzen and Haouari have proposed a bi-objective model for RCPSP with the minimization of the makespan and the maximization of the robustness. The problem was solved by a tabu search heuristic. Chtourou and al. [10] have studied various robustness measures based on priority rules when activity durations vary. The work of Artigues and Leus [11] deals with RCPSP under activity uncertainty. Based on PLNE, the authors proposed a scenario-based bi-level problem formulation that minimizes the absolute and relative regret robustness. The authors have applied, in first, exact method which has taken excessive computational time considering medium sized instances. So they were directed towards heuristic procedures to get better results. In addition, the Genetic algorithm was simply

adapted to robust optimization problems, such as the one machine problem [12] and the robust RCPSP [13]. Heuristics and metaheuristics were also approved as efficient methods for stochastic RCPSP (SRCSP) where the uncertainty is modeled by probabilistic distributions, and the robustness is evaluated in terms of expected makespan. We cite the work of [14] in which metaheuristics were well investigated to SRCPSP, a solution in this work consists in finding an activity-based policy that minimizes the expected makespan. Recently, and based on stochastic methods, the work of [15] gives promising results for RCPSP under uncertainty, in particular, projects with 30 activities.

3.PROBLEM STATEMENT

3.1.Deterministic RCPSP

A deterministic version of RCPSP consists in performing a set A of n activities on a set K of m resources. Every activity i has a fixed processing time denoted by p_i and requires r_{ik} units of resource type k which is characterized by a limited capacity R_k that must not be exceeded during the execution, and activities must not be interrupted. Two additive dummy activities 0 and n + 1 are used that represent to start and the end of the project, respectively. Dummy activities have null time duration and null resource requirement. The objective of the standard RCPSP is to construct a precedence and resources feasible schedule with the minimum makespan. Precedence constraints perform that the start time of an activity i is permitted only when all its previous activities are finished. The Resource constraints satisfy that the use of every resource type, at every instant, does not exceed its capacity.

A schedule S referred to the baseline schedule which is given by the list of activity finish times (start times); let F_i (>=0) denotes the finish time of an activity i, then $S=(F_0, F_1, \ldots, F_n, F_{n+1})$ and the total project duration corresponds to the end project finish time F_{n+1}.

Therefore, the conceptual formulation of the RCPSP is given by the following formula:

$$\min F_{n+1} \text{ sc.} \tag{1}$$

$$F_h \leq F_j - p_j ; j = 1 \cdots n+1; h \in P_j \tag{2}$$

$$\sum_{i \in A(t)} ri_k \leq R_k ; k \in K; t \geq 0 \tag{3}$$

with $A(t)$ denotes the set of activities which are executing at time t, and P_j denotes the set of predecessors of the activity i.

An instance of the RCPSP can be represented by a graph G = (V, E) where the set of nodes V is defined by project activities and E contains arcs according to the precedence relations.

3.2.Min-Max Robust Model

The considered variability for RCPSP relies on activity durations. We use a scenarios-based approach to model the problem variability. Hence, we construct a set of scenarios, denotes by $\sum$, for optimization, let σ_i be a single scenario that corresponds to a problem realization. Each

scenario is found by altering the initial activities durations with respect to a maximal activity delay.

A feasible solution *x* for the robust scheduling problem is represented by an activity list; let *f(x,* σ_i *)* denotes the *makespan* of the generated schedule according to *x* on scenario σ_i. This value defines the local performance of the solution *x* according to σ_i. However, the global optimization process has to find the robust schedule with the global performance across the optimization set. Usually, the global performance is measured in terms of mean value, maximum deviation, etc.
The object of the present work is to optimize the min-max robustness objective of RCPSP which consists in minimizing the maximum makespan value over all scenarios. The optimization objective is given by the following formula.

$$\min \max_{\sigma_i \in \Sigma} (f(x, \sigma_i)) \quad (4)$$

Resource and precedence constraints for the robust RCPSP are the same in the deterministic case (Equations (2) and (3)).

2.3. Complexity

The robust scenario-based robust RCPSP with the min-max robustness objective is an NP-hard problem as it can be reduced to the standard NP-hard deterministic version for a number of scenarios equals to one [6].

4.GRASP METAHEURISTIC

As a multi-start metaheuristic, the GRASP (Greedy Randomized Adaptive Search Procedures) was developed for combinatorial optimization [16, 17]. It consists of an iterative process, in each of one, two phases are performed: a construction phase and a local search phase. The first one permits the construction of a feasible solution iteratively, one element at once iteration. However, the second phase performs the improvement of the recently constructed solution by a simple local search heuristic. The best across all generated solutions is then retained.

In the construction phase, a Candidate List (CL) is generated that contains the set of the candidate elements (edges) to be selected and added to the current partial solution. The CL is ordered with respect to a greedy function that measures the benefit of selecting each element. Moreover, the effective selection of one edge is done from an additive list: the Restricted Candidate List (RCL) that regroups the best elements from the CL with highest greedy values.

The GRASP procedure combines crucial characteristics of search methods. In the one hand, it is adaptive because the greedy function values are updated continuously depending on the current partial solution and the considered schedule construction strategy. In the other hand, it is a randomized-based method such that a selection of one element in the RC L is done randomly.

4. GRASP APPROACH FOR ROBUST RCPSP

In order to overcome the problem complexity, we propose to investigate metaheuristics, in particular, to apply a GRASP approach to the RCPSP with the optimization of the absolute robustness so called the min-max robustness objective.

The main steps of the proposed approach are depicted in the following figure. As a multi-start heuristic, the algorithm starts with generating gradually a new solution. This step integrates an intensification strategy. Current solution is improved, in the second step, by a Local Search heuristic (LS), and a Forward-Backward Improvement (FBI) heuristic.

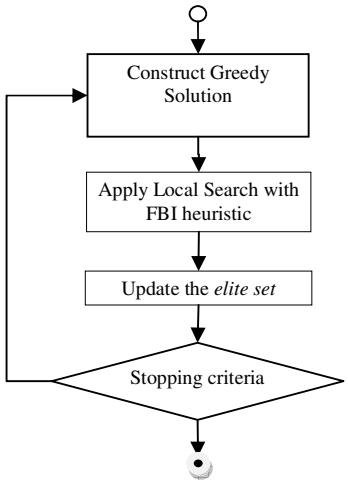

Figure 1. General steps of the enhanced GRASP approach

Throughout this iterative process a vector ES is generated which contains the best encountered solutions (elite set). The size of the *ES* is defined by a fixed parameter denoted by *nbElite*. Elite solutions are updated iteratively.

4.1. Solution Representation and robust fitness

A solution is represented by an activity list that satisfies precedence constraints. To evaluate the global solution performance, a *robust evaluation* is made. We apply decoding procedure to generate the schedule according to the activity list *x* and the scenario σ_i. Then, the *robust fitness* which measures the global solution performance is determined by the maximum makespan over all obtained values for $\sum$. The Serial Schedule Generation Scheme (Serial SGS) is used as a decoding procedure [2] to construct the schedule.

4.2. Construction Phase

At one iteration of the construction phase one activity is selected from an eligible set an added to the current partial solution. We generate the list CL of candidate activities having all their predecessors scheduled. For each activity in the CL, the corresponding greedy function value is equals to the priority rule value. We propose the application of different priority rules: the minimum Latest Finish Time (MLFT), the minimum of the activity free slack (MFLK), the inverse free slack priority rule, and the critical activity based selection. The object is to study the effect of the priority rule on robustness objective.

First activities of the CL are then copied in the *RCL*. The size of the latter list is denoted by *TRCL*. From the constructed RCL, an activity is then chosen randomly and added at the latest position in the partial activity list. A pool of elite solutions *ES* is constructed.

To ensure solutions with a high quality, we incorporate in the construction phase an intensification strategy based on the elite set. When the *ES* attempts the fixed parameterized size, then, with probability *pES*, we select randomly one element to be considered at the current iteration of the construction phase. Then, the first activity, in the elite solution, that does not appear in the partial current solution is selected and inserted in. The above described process is repeated until the construction of the totality of the solution is reached. Figure 2 gives the pseudo code of the proposed greedy construction procedure, we suppose that ES contains at least one element.

```
procedure ConstructGreedyRandomizedSolution(S)
    S = {};
    for Solution construction not done do
        p=random();
        if (p<pES)
            S' = SelectElementAtRandom (ES)
            e = select First Element in S' and doesn't appear in S
        else
            MakeRCL(CL, TRCL, RCL);
            e = SelectElementAtRandom(RCL);
        end
        S = S ∪{e};
    end
end ConstructGreedyRandomizedSolution.
```

Figure 2. Pseudo code for the proposed GRASP construction phase

4.3. Improvement Phase

The proposed GRASP improvement phase combines a Local Search procedure (LS) with a FBI heuristic. The proposed Local Search starts from the recently constructed and improved solution x. Iteratively, a local move is applied to x to generate a neighbourhood set: N(x). The proposed move consists of the permutation of one activity of x with others nodes. The activity to be permuted is chosen at random. Obtained feasible solutions are saved to be compared with x. The best element over all neighbours and the current solution is retained. After a maximum number of iterations, the search method would stop with the best solution over all neighbourhoods.

The Forward-Backward Improvement (FBI) method is a two-passes method which was used by Li and Willis (1962) for project scheduling. Starting with a schedule generated by a serial SGS, we apply, alternatively, forward and backward recursion using the Serial SGS. Resulting schedule in one pass is updated and used as a priority list in the next pass [2, 18].

5. COMPUTATIONAL EXPERIMENTS

5.1. Data Sets and Robust Parameters Setting

The proposed enhanced GRASP approach was implemented in Java and ran on a portable personnel computer equipped with an Intel® Core™ i5-2450M CPU@ 2.50 GHz 773MHz, 2.70Go of RAM. Experiments were performed on two benchmark project instances: the Patterson data set [19], and the PSPLIB J30 data set [20]. The first data set contains 110 instances of various projects with 3 resource types and a number of activities that vary between 6 and 51. The

second data set contains 480 project instances which are generated by the ProGen generator. These instances represent different projects with only 30 activities and 4 resource types.

Scenarios are generated with limited size for both the optimization and the evaluation (simulation) set. The optimization set contains *nbScen* scenarios, equals to 10, used to compute the robustness objective. The evaluation set is used for simulation to estimate the expected makespan. The size of the evaluation set is denoted by *l*. A scenario is an initial problem realization where a set of activities are modified by altering their initial durations. In fact, for 10 percent of the total project activities, we add a time increment δ which is taken from a uniform distribution U(1, *maxDelay*). The latter parameter indicates the maximum activity delay which is fixed to 10.

5.2. Performance measures

To evaluate the performance of the proposed GRASP robust approach, we were interested by the following performance measures:

- The estimate *Expected makespan* which is calculated over the evaluation set $\left(\mathrm{E}(\mathrm{C}_{\max}) = \frac{1}{l}\sum_{i=1}^{l}(f(x,\sigma_i))\right)$;
- The *Standard deviation* of the makespan over the evaluation set;
- The *Relative Optimality gap* that measures the deviation between the estimate expected makespan and the lower bound *LB*, or the optimal makespan if exists, for the corresponding deterministic project $\left(\frac{E(\mathrm{C}_{\max})-LB}{LB}\right)$.

All results are averaged by the number of tested project instances.

5.3. Evaluation in Deterministic Case

We started experiments by testing the GRASP approach in the deterministic case. Hence, Table 1 shows results on the J30 data set. We performed the basic GRASP approach which is based on a Local Search (LS) in the improvement phase (column 2). Then, the basic algorithm is improved with the FBI and tested for the same instances set. We vary the maximum number of iterations for both GRASP process (Line 2), and the LS (Line 3). Line 4 reported the average deviation from the well-known optimal solutions in percent, for both two GRASP implementations. The number of the obtained optimums is given in Line 5.

Table 1. Average deviations from optimal solutions J30 data set instances (the deterministic case).

	GRASP-LS	**GRASP-LS+BFI**			
Iterations for GRASP	100	100	300	3000	1000
Iterations for LS	100/2	10	10	10	1000/4
Optimality deviation	0.51	0.57	0.34	0.24	0.20
Optimums	396	390	419	428	434

Results for the static RCPSP show the performance of the applied GRASP procedure compared with other methods in the literature [3], especially when combined with the forward-backward improvement heuristic.

5.4. Evaluation of the Proposed Robust Approach

Under uncertainty, we have performed different runs of the proposed GRASP on Patterson data set. The basic algorithm denoted as (GRASP-LS(10)) is considered as the implementation of the GRASP approach with the LFT priority rule in the construction phase and 10 iterations of local search procedure. We vary the maximum number of iterations with the local search incorporated in GRASP.

Table 2. Robustness evaluation on Patterson data set (1000 simulations).

	GRASP-LS(10)	**GRASP-LS(20)**	**GRASP-LS(100)**
Avg. Optimality gap	0.2366	0.2384	0.2249
Avg. Standard deviation	3.4423	3.4026	3.4121

Results are reported in Table 2 with 1000 simulations as the size of the evaluation set. The simulation procedure was run for each project instance. We observe that the local search procedure has an impact on the global performance. In fact, an increment of the number of iterations yields to better results for robustness. However, this parameter must be controlled to ensure the non degradation of the later objective, which is the case with 100 iterations in the local search procedure.

To evaluate the influence of the FBI heuristic on the global GRASP performance, Table 3 contains numerical results on J30 data set under uncertainty, simulated over 100 replications. We point out that the enhanced GRASP (Column 2) outperforms the basic version with a minimum value of the average standard deviation.

In parallel, we try to examine the performance of proposed approach compared with an evolutionary-based robust solution from the literature. Hence, we consider the robust genetic algorithm proposed in [13] for RCPSP under uncertainty. Colum 3, in table 3, reports results of that evolutionary approach applied, with the same robustness objective, to the same data set. For this tested algorithm, the stopping criterion is to attempt 1000 generated schedules. The GRAS approach improved with the FBI heuristic gives better results than the evolutionary algorithm with the same maximum number of generated schedules.

Table 3. Robustness evaluation on J30 data set (100 simulations).

		GRASP-LS(10) (500 iter)	**GRASP-LS(20) + BFI (250 iter)**	**Evolutionary Algorithm**
Optimality gap	**avg.**	0.1349	0.1243	13.46
	max.	0.2755	0.2603	27.05
Standard deviation	**avg.**	4.2515	4.1428	4.2386
	max.	6.3863	5.8086	5.5664

We performed different runs of based GRASP approaches, and evaluated the computational time on Patterson instances set for 1000 generated schedules. The corresponding results are shown in Table 4. As described in [18], the FBI heuristics needs two passes of the SGS procedure to doubly justified the initial schedule. Thus, the number of generated schedules with the basic GRASP algorithm and the enhanced version with a FBI heuristic is equals to$(\mathrm{nbIterMax} \times 10)$,

and$(\text{nbIterMax} \times (10 + 3))$, respectively. Column 2 and 3, in this table, show that, for maximum 1000 generated schedules, the enhanced GRASP outperforms the basic GRASP in terms of robustness and computational time.

Table 4. Comparison between GRASP and GRASP-FBI on Patterson data set (1000 simulations).

		GRASP-LS(10)	**GRASP-LS(10) + BFI**	**GRASP-LS(10) + BFI**
Nunber of iterations		100	75	333
Optimality gap	**avg.**	0.2362	0.2304	0.2259
	max.	1.3352	1.31197	1.3398
Standard deviation	**avg.**	3.4106	3.4008	3.4089
	max.	5.5832	5.6207	5.5526
Time(s)		2.04	1.775	7.926

5.5. Priority Rule on Schedule Construction

The idea of the present experiment is to study the effect of priority rules on robustness solution quality. As described in section 4, the construction phase implements a priority rule to order the Candidate List content, from which we select the TRCL best elements to the RCL.

We investigate in table 5 different priority rules based on critical path: Minimum Latest Finish Time (MLFT), the minimum Slack (MSLK), the inverse MSLK, the critical Activity based rule. The total activity slack is obtained by the difference between its latest and earliest start time. We also propose to study a priority rule which based on graph structure which is the GPRW (Greatest Rank Positional Weight). We ran the GRASP algorithm with two different RCL size values (TRCL).

Table 5. The Standard deviation variation on Patterson data set (1000 simulations).

	GRASP-LS(10)	
Priority rule	**TRCL=5**	**TRCL=3**
MLFT	3.4721	3.4456
MSLK	3.4702	3.4871
inverse MSLK	3.4640	3.4454
Critical Activity	3.4533	3.4741
GPRW	3.4606	3.4499

With limited size of the restricted list, the standard deviation of the estimated makespan is decreased as we reinforce best elements in the RCL. The inverse MSLK gives better results than the MSLK; this result can be interpreted as the inverse SLK favour activities having greatest slack values, consequently generated schedule will be more flexible to absorb activity delays.

6. CONCLUSIONS

In this article, we have studied the RCPSP with activity duration uncertainty. Based on scenarios, the object of the tackled problem is to optimize the min-max robustness objective. We have proposed an enhanced GRASP method which incorporates priority rules in the greedy construction phase and a local search with a forward-backward heuristic in the improvement

phase. Our robust approach was successfully tested in both deterministic and robust cases; the combination of the GRASP with the FBI has improved the robustness objective. Moreover experiments have shown the simplicity and the efficiency of our robust approach compared with other complex metaheuristic such as evolutionary-based approach. Further works should be focused on the investigation of more metaheuristics approaches in robust project scheduling, and therefore exploit more large-sized project instances.

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