

# DESIGN AND IMPLEMENTATION OF COMBINED PIPELINING AND PARALLEL PROCESSING ARCHITECTURE FOR FIR AND IIR FILTERS USING VHDL

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## ABSTRACT

Along with the advancement in VLSI (Very Large Scale Integration) technology, the implementation of Finite impulse response (FIR) filters and Infinite impulse response (IIR) filters with enhanced speed has become more demanding. This paper aims at designing and implementing a combined pipelining and parallel processing architecture for FIR and IIR filter using VHDL (Very High Speed Integrated Circuit Hardware Descriptive Language) to reduce the power consumption and delay of the filter. The proposed architecture is compared with the original FIR and IIR filter respectively in terms of speed, area, and power. Also, the proposed architecture is compared with existing architectures in terms of delay. The implementation is done by using VHDL codes. FIR and IIR filters structures are implemented at 1200 KHz clock frequency. Synthesis and simulation have been accomplished on Artix-7 series FPGA, target device (xc7a200tfbg676) (speed grade -1) using VIVADO 2016.3.

## KEYWORDS

DSP, FIR, FPGA, IIR, MIMO.

## 1. INTRODUCTION

A filter is one of the basic signal processing circuits used in communication systems and physical applications. Filters are the electronic circuits which allow or transmit the desired band of frequencies and attenuate the unwanted band of frequencies. Digital filters process and generate digital data. Digital filters consist of elements like adder, multiplier and delay unit. The properties of a causal digital filter can be completely characterized by its unit-sample response  $h(n)$ , or its transfer function  $H(z)$ , or by difference equations [1]. Difference equation representations definitely show the computations required to implement the filter. The transfer function for a linear, causal and time-invariant, digital filter can be expressed as a transfer function in the  $z$ -domain as:

$$H(z) = \frac{B(z)}{A(z)} = \frac{b_0 + b_1z^{-1} + b_2z^{-2} + \dots + b_Nz^{-N}}{1 + a_1z^{-1} + a_2z^{-2} + \dots + a_Mz^{-M}} \quad (1)$$

Where the order of the filter should be greater than N or M.

In discrete-time systems, the digital filter is often implemented by converting the transfer function to a linear difference equation. The resultant linear difference equation is: [2]

$$y(n) = -\sum_{k=1}^N a_k y(n-k) + \sum_{k=0}^M b_k x(n-k) \quad (2)$$

High-performance digital filter is the need for digital signal processing. The speed of a filter realization depends not only on the potentialities of the hardware platform on which it is employed, but as well on the computational structure of the code [3].

The objective of the paper is to design and implement a combined pipelining and parallel processing architectures on FIR and IIR digital filters to achieve high-speed or low power consumption.

This paper is organized as follows: In Section 2 and 3, the FIR and IIR filter are discussed. Pipelining and parallel processing techniques are discussed in Section 4 and 5. In Section 6, literature survey is presented. In Section 7, implementation of the combined pipelining and parallel processing is discussed. Simulation results and performance analysis of the implemented architectures are discussed in sections 8 and 9. Conclusions are given in Section 10.

## 2. FIR FILTER

The FIR digital filter is widely used in DSP systems, ranging from wireless communications to video and image processing [4]. FIR filters are non-recursive filters as there is no feedback involved. All paths connecting the input to the output flows in the forward direction, so the signal flow is strictly feed-forward in FIR Filter.

The difference equation for the FIR filter which defines the relation of the input signal to the output signal is given as

$$y(n) = b_0 x(n) + b_1 x(n-1) + \dots + b_N x(n-N) \quad (3)$$

It can also be expressed as

$$y(n) = \sum_{i=0}^N b_i x(n-i) \quad (4)$$

Where  $x(n)$  is the input signal,  $y(n)$  is the output signal,  $b_i$  is the filter coefficients and  $N$  is the filter order [5].

In an FIR filter, DSP microprocessors feature multiply-accumulate (MAC) units since adders for additions are required in combination with multiplier for the multiplications. Based on the multiplication and accumulation of filter coefficients, the accuracy of designing a filter is determined. FIR filters are the causal, linear and time-invariant systems.

The realization of FIR filter in transpose form configuration is required. Transpose form FIR filter preserves the functionality of the filter and overcomes the computational delay problem of the direct form FIR Filter [6].

### 3. IIR FILTER

IIR filters have feedback loop (a recursive part of a filter) so they are also called as recursive filters. The difference equation for IIR filter that defines how the output signal is related to the input signal is given as

$$y(n) = \frac{1}{a_0} \left( \sum_{i=0}^P b_i x(n-i) - \sum_{j=1}^Q a_j y(n-j) \right) \quad (5)$$

The transfer function is defined as

$$H(z) = \frac{Y(z)}{X(z)} = \frac{\sum_{i=0}^P b_i z^{-i}}{\sum_{j=0}^Q a_j z^{-j}} \quad (6)$$

Considering that in most IIR filter designs coefficient  $a_0$  is 1, the IIR filter transfer function can be rewritten as

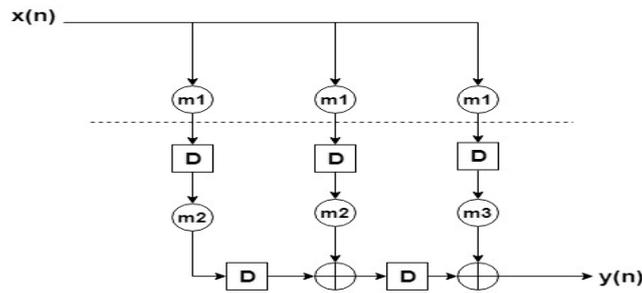
$$H(z) = \frac{Y(z)}{X(z)} = \frac{\sum_{i=0}^P b_i z^{-i}}{1 + \sum_{j=1}^Q a_j z^{-j}} \quad (7)$$

where P is the feed-forward filter order,  $b_i$  is the feed-forward filter coefficients, Q is the feedback filter order,  $a_j$  is the feedback filter coefficients,  $x(n)$  is the input signal and  $y(n)$  is the output signal [7].

IIR filters are better to implement than FIR filters to meet the specifications like pass band, stop band, etc. Computation time is saved by using digital IIR filters which is a large factor. IIR filters are computationally more efficient than FIR filters as they require fewer coefficients due to the usage of poles and feedback [21].

### 4. PIPELINING

Pipelining is an implementation technique where a stream of instructions are executed simultaneously and results in speed enhancement for the critical path by reducing the critical path delay in most of the DSP system [8]. Pipelining accumulates the instructions from the processor making the processors fast [5]. By using pipelining technique, critical path can be reduced, which in turn increases the sample speed and throughput of the system. It can also be used to reduce power consumption at the same speed [1] [4].



**Figure 1.** Fine-grain pipelining of a 3-tap FIR filter.

In the FIR filter, the pipeline latches are introduced across any feed-forward cutset without changing the transfer function at the expense of latency. This is referred to as fine-grain pipelining. Figure 1 shows a fine-grain pipelining of a 3-tap FIR filter. In an M-level pipelined system, the number of delay elements in any path from input to output is (M-1) greater than the delay element in the original sequential circuit [1].

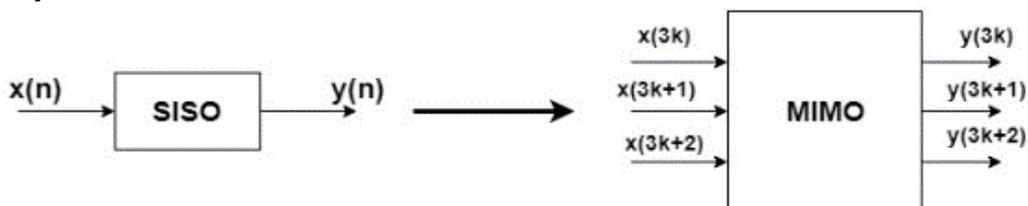
In IIR filter, simply inserting pipelining latches alter the loop delay which leads to a change in the transfer function. Hence, in order to pipeline an IIR filter while conserving its original transfer function, the computations must first be redeveloped into what is called a look-ahead filter form[5][9]. IIR filters are pipelined using look-ahead techniques and decomposition technique which is discussed in [10]. This reformulation provides additional delays in the feedback loop that can be used to balance the pipeline stages by introducing a new cancelling pole and zero for each additional register inserted.

Pipelining does not accelerate instruction execution time, but it does accelerate program execution time by increasing the number of instructions finished per unit time [5] [8] [4].

There is a limitation in pipelining which is imposed by the input/output (I/O) bottlenecks. This essentially means that pipelining can be used only to the extent such that the critical path computation time is limited by the communication or I/O bound, and once the system is communication bounded, pipelining can no longer increase the speed of the system. Once the system is communication bounded, pipelining can be combined with parallel processing to further increase the speed of the architecture [1].

## 5. PARALLEL PROCESSING

Parallel processing is an implementation technique in which multiple outputs are computed in parallel in a clock period. In parallel processing, the hardware for the original serial system is duplicated and the resulting system is a MIMO (multiple inputs multiple outputs) parallel system. Figure 2 shows the block diagram of conversion of SISO (single input single output) system to a MIMO system.



**Figure 2.** Sequential system to 3-parallel system.

Parallel processing systems are also referred to as block processing systems. Because of the MIMO system, placing a latch at any path produces a delay of  $L$  clock cycles. In the block structure with block size  $L$ , each implementable latch is  $L$ -slow, i.e., the clock rate of the latch in the block filter is  $L$  times slower than the input sample rate. If an  $L$  parallel filter is operated,  $L$  output samples are generated every clock period whereas in the original filter single output sample is generated in every clock period. This implies that the  $L$ -parallel filter effectively operates at  $L$  times the rate of the original filter [11] [12]. In parallel filter, the sampling frequency is increased while the frequency of the clock remains the same. Therefore, the effective sampling speed of the system is increased by the level of parallelism [1].

Parallel processing is a robust technique because it can be used to increase the throughput of a digital filter or to reduce the power consumption of a digital filter [11] [13]. The block processing method not only increases the throughput of the system but also improves area-delay efficiency.

In IIR filter, in straightforward implementation of parallel processing, the hardware complexity is  $L^2$  multiply-add operations since  $L$  multiply-add operations are required for each output and there are  $L$  outputs in total. The incremental block processing technique can be used to reduce hardware complexity. In the incremental computation, the outputs are incrementally computed in a sequential manner using the non-recursively computed intermediate states [14]. The hardware complexity has been reduced to  $2L - 1$  from  $L^2$  at the expense of an increase in the system latency [1].

Parallel processing is used for the reduction of power consumption while using slow clocks. This reduces the power consumption due to the clock lines as compared with a pipelined system, which needs to be operated using a faster clock for equivalent throughput or sample speed.

## 6. RELATED WORK

In [5], the author uses the technique of pipelining to measure the efficiency of an algorithm. The author uses different FPGAs to perform a comparative study between pipelined & non-pipelined FIR and IIR filters. The results show that the implemented pipelined filter improves the overall speed of the filter than the non-pipelined filter. In [20], for high throughput applications, the author implemented four different structures: unfolded direct form parallel architectures(UDFPA), unfolded broadcast form parallel architectures(UBFPA), parallel retimed broadcast architecture (PRBA) and parallel systolic architecture (PSA) with varying levels of parallel and pipelined implementations of finite impulse response (FIR) filter using different FPGAs. The author concluded that PSA has a better resource utilization based in terms of area-delay product and power-delay product. In [3], the author proposes an FPGA based design of exceedingly high-speed notch filter which practically operates at a maximum clock frequency of 1200MHz using Scattered-Look-Ahead (SLA) pipelining with a power-of-2-decomposition approach. The author also proposes a new efficient simpler approach for calculating the coefficients of the multiplier of both feed-forward and feedback portions of an exceedingly high-speed notch filter using Pascal's Triangle. The proposed work is applicable in communication as well as in the non-communication field where noise elimination is necessary. In [19], a 4-tap sequential and parallel micro-programmed based digital FIR filter have been implemented with the help of a 16 bit Wallace tree multiplier and a 16 bit Vedic multiplier using VHDL codes. Based on the implementation results obtained through FPGA synthesis tools performance of the filter is evaluated. The author observes that the sequential filter achieves better performance with reference to speed and resource utilization than the parallel filter. Also, Vedic multiplier is faster than Wallace multiplier.

## 7. PROPOSED WORK

### 7.1. Implementation of 3-Tap FIR Filter

The difference equation of the 3-tap FIR filter can be expressed as

$$y(n) = ax(n) + bx(n-1) + cx(n-2) \tag{8}$$

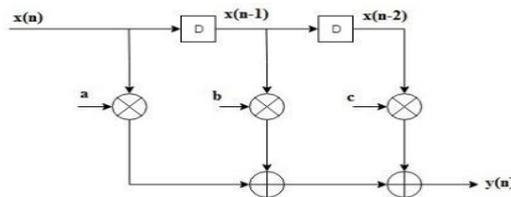


Figure 3. Direct form 3-tap FIR Filter [1].

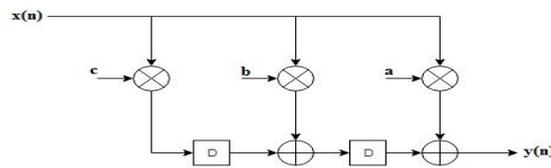


Figure 4. Transposed form 3-tap FIR Filter [1].

The direct form structure and transposed form structure of 3-tap FIR filter is shown in Figure 3 and Figure 4 respectively. The transposed form 3-tap FIR filter is implemented at 1200 kHz frequency using VHDL codes. The 1200 kHz clock frequency is derived from the system frequency of 50 MHz.

### 7.2. Implementation of Combined Parallel-Pipelined FIR Filter

The parallel structure of the 3-tap FIR filter is shown in Figure 5.

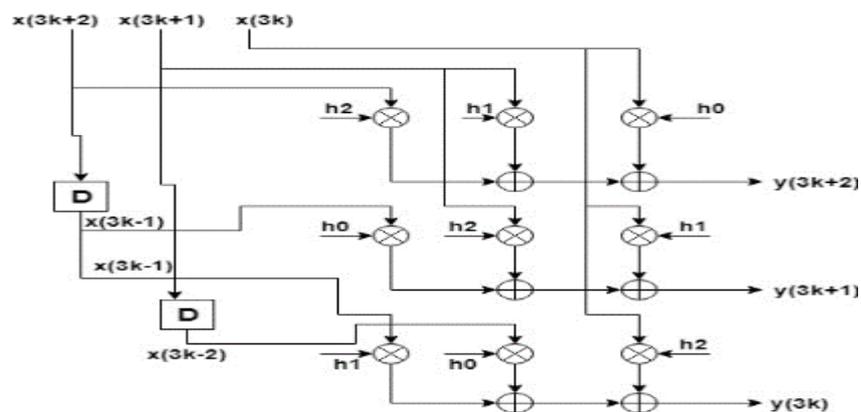


Figure 5. Parallel structure for 3-tap FIR filter [1].

The difference equation of the parallel FIR is

$$y(3k) = h_2x(3k) + h_0x(3k - 2) + h_1x(3k - 1)$$

$$y(3k + 1) = h_1x(3k) + h_2x(3k + 1) + h_0x(3k - 1)$$

$$y(3k + 2) = h_0x(3k) + h_1x(3k + 1) + h_2x(3k + 2)$$

For implementing a combined parallel-pipelined structure, the sequential system is converted into a parallel system by using a serial to parallel converter. In a MIMO system the inputs are generated using the 3600 kHz frequency clock. The multiplier in the parallel structure is broken into two smaller units by fine grain pipelining. This parallel-pipelined structure is implemented using VHDL codes at 1200 kHz clock frequency. Here, the level of parallelism used is 3 and that of pipelining is 2. Hence, three outputs are generated in every clock cycle.

Combined pipelined and parallel processing architecture for 3-tap FIR filter is shown in Figure 6.

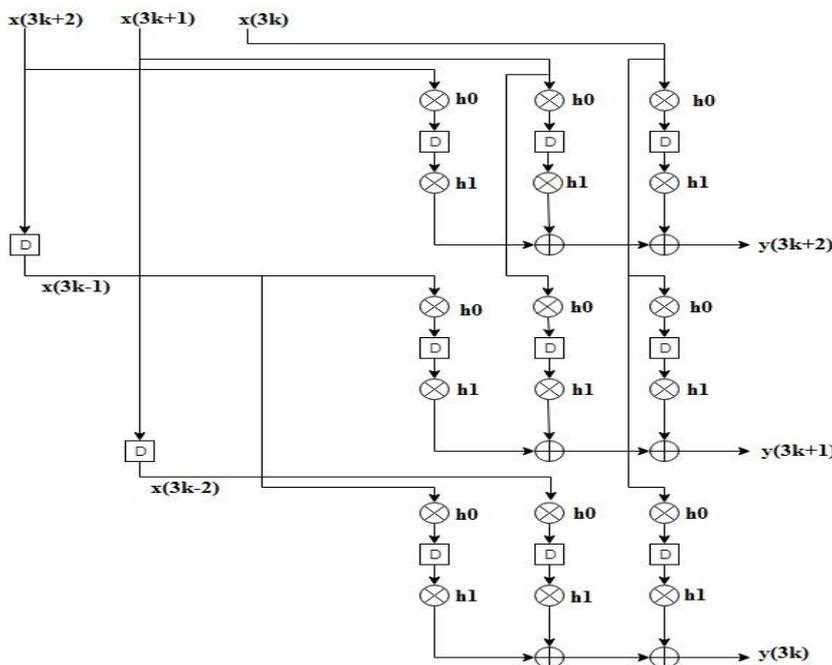


Figure 6. Combined pipelined and parallel processing architecture for 3-tap FIR filter.

### 7.3. Implementation of 1<sup>st</sup> Order IIR Filter

Since it is 1<sup>st</sup> order IIR filter, it has only one pole at 'a'. The value of |a| should be less than or equal to 1 for the system to be stable (here the value of a is assumed to be 0.5).

$$y(n) = ay(n - 1) + x(n) \tag{9}$$

It can also be expressed as

$$y(n) = 0.5y(n - 1) + x(n)$$

From the difference equation, the 1<sup>st</sup> order IIR filter is implemented at 1200 kHz clock using VHDL codes. Figure 7 shows the block diagram of the 1<sup>st</sup> order IIR filter.

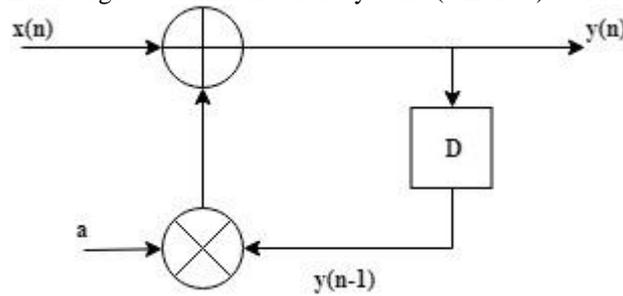


Figure 7. 1<sup>st</sup> order IIR filter [1].

### 7.4. Design and Implementation of Combined Parallel-Pipelined IIR Filter

Like the FIR filter, 1<sup>st</sup> order IIR filter is converted into the parallel system and inputs are generated at 3600 kHz frequency clock. The parallel structure of the IIR filter is shown in Figure 8.

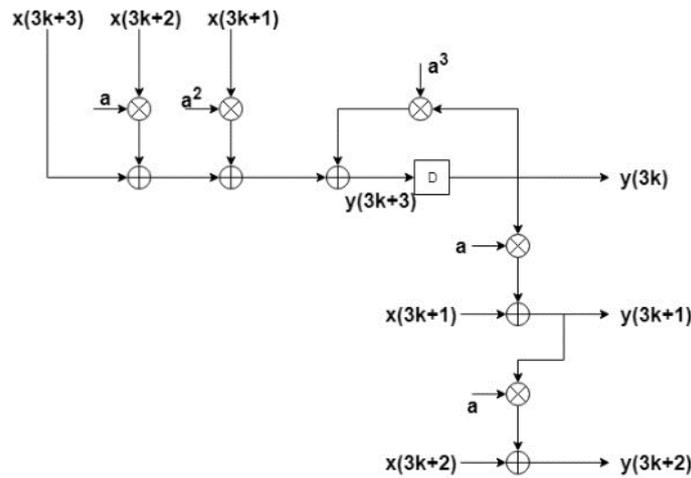


Figure 8. Parallel structure of IIR filter.

The difference equation of parallel IIR filter is derived from the 1<sup>st</sup> order IIR filter. From the difference equation of 1<sup>st</sup> order IIR filter (7.2)

$$\begin{aligned}
 y(n) &= ay(n-1) + x(n) \\
 y(3k+3) &= ay(3k+2) + x(3k+3) \\
 y(3k+3) &= a[ay(3k+1) + x(3k+2)] + x(3k+3) \\
 y(3k+3) &= a^2y(3k+1) + ax(3k+2) + x(3k+3) \\
 y(3k+3) &= a^2[ay(3k) + x(3k+1)] + ax(3k+2) + x(3k+3) \\
 y(3k+3) &= a^3y(3k) + a^2x(3k+1) + ax(3k+2) + x(3k+3)
 \end{aligned}$$

Since L=3, it is expressed in 3k and (3k+3) because (3k+3) delayed by one clock gives 3k.

The parallel-pipelined IIR Filter is designed by deriving the difference equation. The proposed design is implemented at 1200 kHz clock frequency with the level of parallelism (L) 3 and stages

International Journal of VLSI design & Communication Systems (VLSICS) Vol 10, No 4, August 2019 of pipelining (M) 2. The inputs are generated at 3600 kHz clock. Figure 9 shows the combined pipelining and parallel processing architecture for IIR filter.

From the difference equation of the 1<sup>st</sup> order IIR filter (7.2)

$$y(n) = ay(n-1) + x(n)$$

Since M=2, we have to add one more delay to the original sequential filter and L=3, hence (3k). So (3k+6) delayed by two cycles gives (3k).

Therefore,

$$y(3k+1) = ay(3k) + x(3k+1)$$

$$y(3k+2) = ay(3k+1) + x(3k+2)$$

.

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$$y(3k+5) = ay(3k+4) + x(3k+5)$$

$$y(3k+6) = ay(3k+5) + x(3k+6)$$

Substituting the values, we get

$$y(3k+6) = a^6 y(3k) + a^5 x(3k+1) + a^4 x(3k+2) + a^3 x(3k+3) + a^2 x(3k+4) + ax(3k+5) + x(3k+6)$$

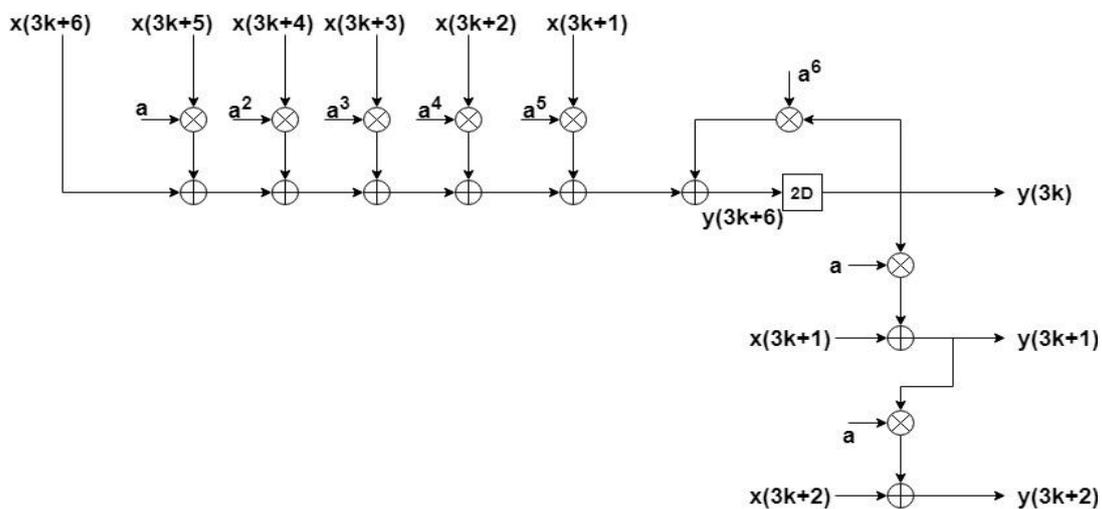


Figure 9. Combined pipelined and parallel processing architecture for 1<sup>st</sup> order IIR filter.

The proposed combined pipelining and parallel processing architecture for IIR Filter is designed and implemented.

The results of the implemented designs are being analyzed in the latter section of this paper.

## 8. EXPERIMENTAL RESULTS

The register transfer level (RTL) schematic of 3-tap FIR filter is shown in Figure 10. The simulation output waveform of the 3-tap FIR filter is shown in Figure 11. In this Fig, clk\_1200khz represents the 1200 kHz frequency clock, xin represents the 8 bit input sample and yout represents the 16 bit output.

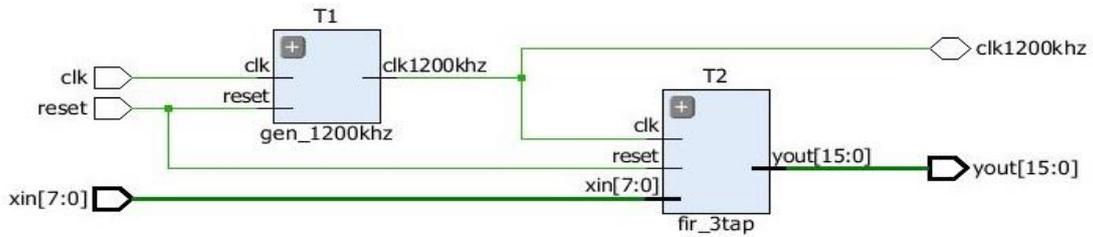


Figure 10. RTL schematic of 3-tap FIR filter.



Figure 11. Simulation waveform of 3-tap FIR filter.

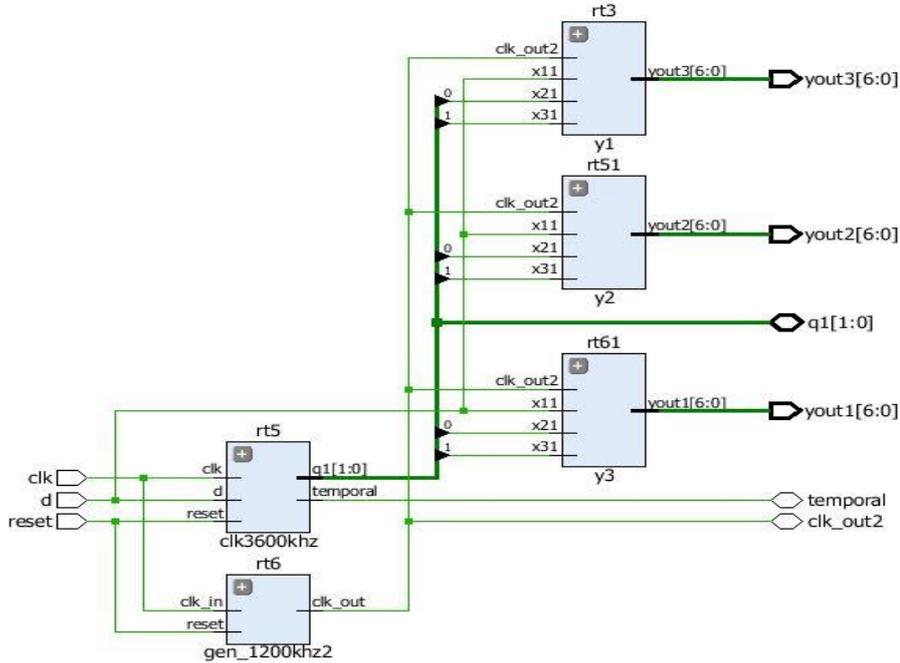


Figure 12. RTL schematic of the combined pipelining and parallel processing FIR architecture.

Figure 13 shows the simulation waveform of the combined pipelined and parallel processing architecture. Here, temporal represents 3600 kHz frequency clock and clk\_out2 represents the 1200 kHz frequency clock, d is the data applied and q is the inputs which are generated in parallel. Yout1, Yout2 and Yout3 represent  $y(3k)$ ,  $y(3k+1)$  and  $y(3k+2)$  respectively. Since  $L=3$ , three outputs are generated in a single clock cycle.

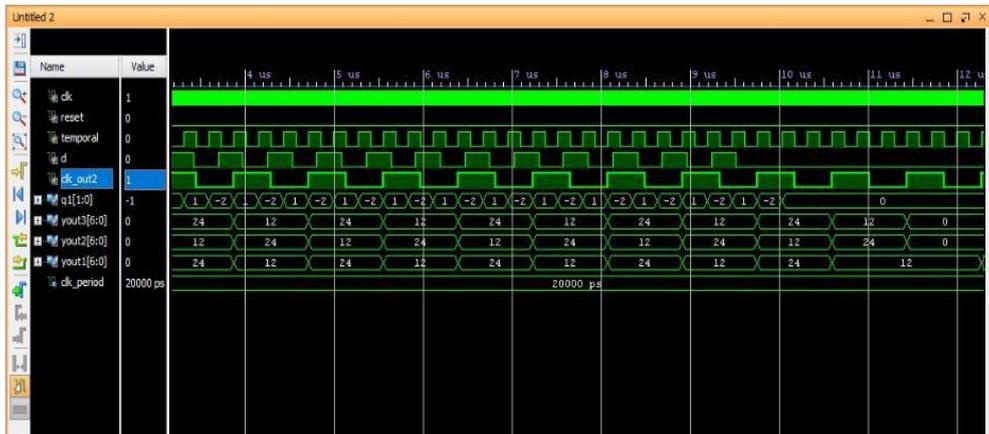


Figure 13. Simulation waveform of the parallel-pipelined FIR filter.

The RTL schematic of 1<sup>st</sup> order IIR filter is shown below in Figure 14.

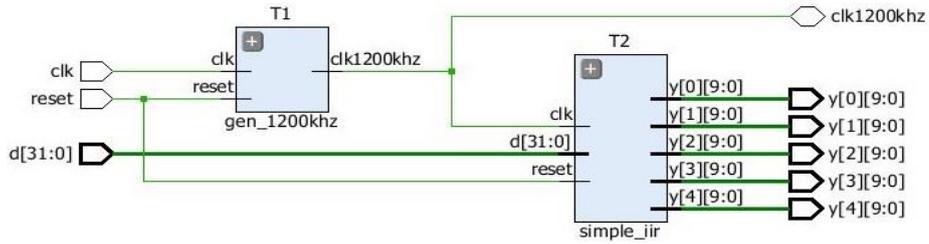


Figure 14. RTL schematic of 1<sup>st</sup> order IIR filter.

Figure 15 shows the simulation waveform of the 1<sup>st</sup> order IIR filter. In this fig, clk\_1200khz represents the 1200 kHz frequency clock, d is the data and y is the output which is generated as an array of data.

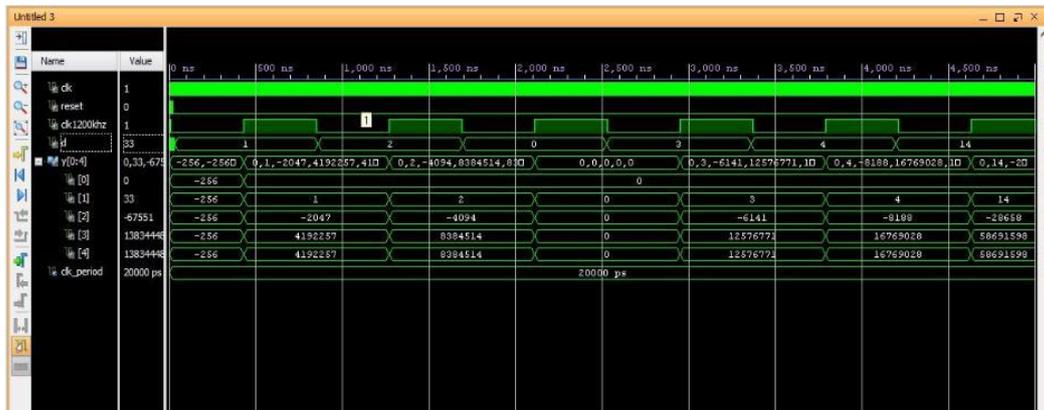


Figure 15. Simulation waveform of 1<sup>st</sup> order IIR filter.

The RTL schematic of the combined pipelining and parallel processing IIR filter is shown in Figure 16.

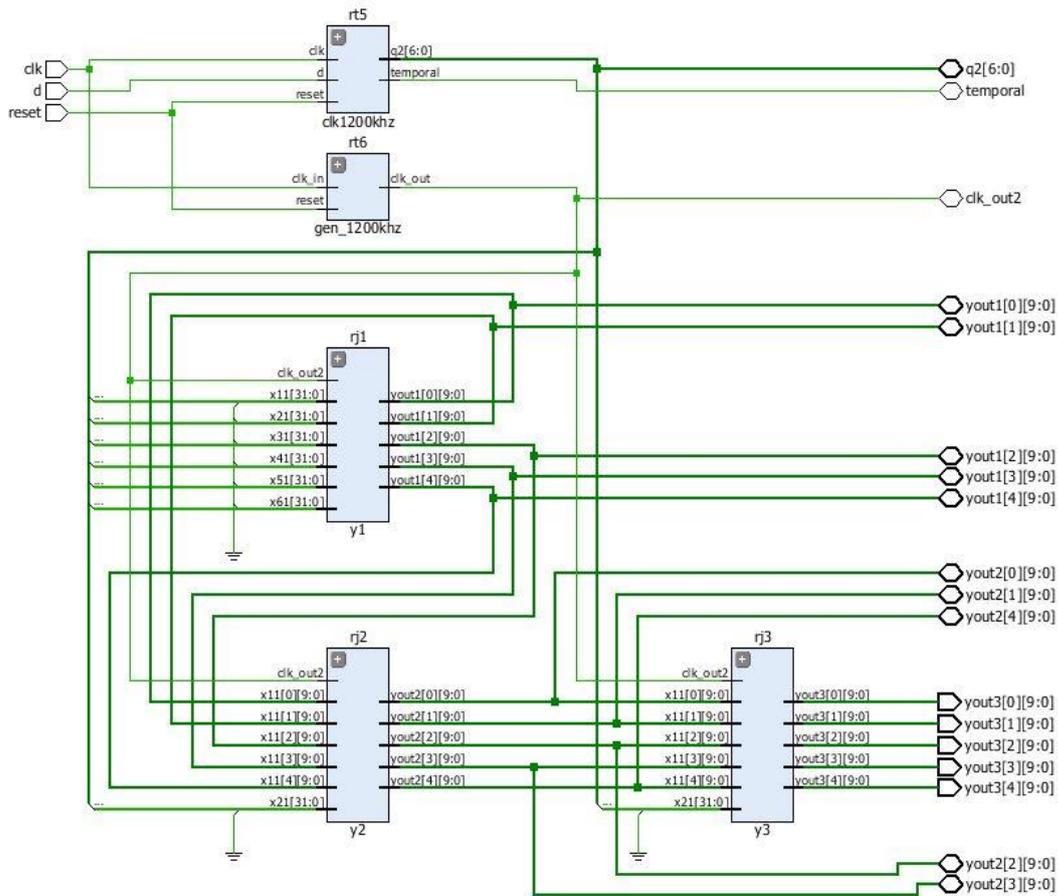


Figure 16. RTL schematic of the combined pipelined and parallel processing IIR architecture.

Figure 17 shows the simulation waveform of the combined pipelined and parallel processing IIR architecture. Here, temporal represents 3600 kHz frequency clock and clk\_out2 represents the 1200 kHz frequency clock, d is the data applied and q2 is the inputs which are generated in parallel. Yout1, Yout2 and Yout3 represents  $y(3k)$ ,  $y(3k+1)$  and  $y(3k+2)$  respectively. Since  $L=3$ , three outputs are generated in a single clock cycle; outputs are generated as an array of data.

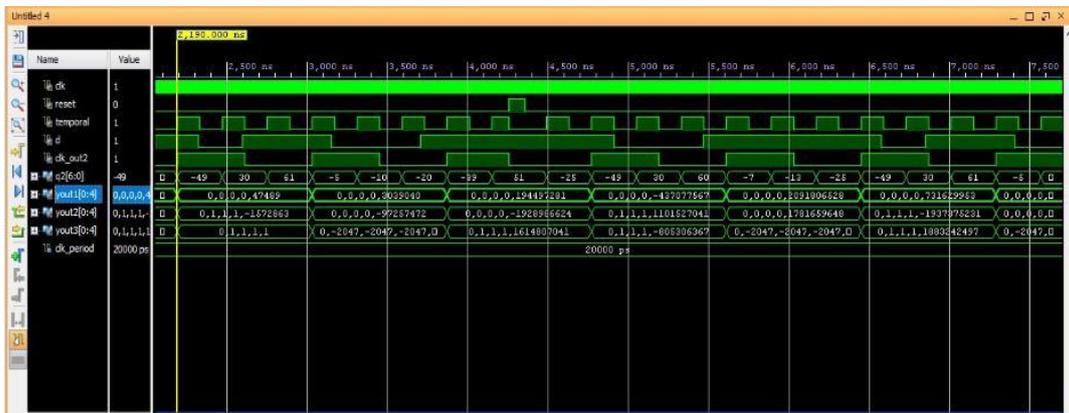


Figure 17. Simulation waveform of parallel-pipelined IIR filter.

From the simulation results, we can see that three outputs are generated in every clock period since the level of parallelism applied is 3. The inputs for the combined architectures for both FIR and IIR digital filters are generated at 3600 kHz clock frequency and the outputs are generated at 1200 kHz frequency since the proposed architecture works at 1200 kHz clock frequency. From the synthesis and utilization reports, the area in terms of look up table (LUT), power consumption and delay of the architecture is analyzed. After analyzing, we can conclude that the combined architectures consumes less power and has less delay for both FIR and IIR filter hence, speed is enhanced in the proposed architecture.

## 9. PERFORMANCE ANALYSIS

Table1. Synthesis results of FIR and IIR filters

SL.NO.	FIR 3-tap	Par-pip FIR	IIR 1 <sup>st</sup> order	Par-pip IIR
Area (in terms of LUT)	38 out of 133800	21 out of 133800	4 out of 133800	6 out of 133800
Power	15.152W	8.053W	10.375W	5.293W
Delay	9.347ns	5.124ns	4.255ns	4.724ns

From the Table 1, we observed that at the same clock frequency i.e. 1200 kHz, the pipelined and parallel FIR filter has less area, power consumption, and delay which mean that the speed is increased as compared to the original 3-tap FIR filter. For the IIR filter at 1200 kHz clock frequency, we have found that with a slight increase in area, power consumption in the filter is reduced with less or approximately equal speed.

Table2. Comparison between the existing structure and the proposed architecture

Structures	Delay(ns)	
	16 bit Vedic multiplier [19]	4-tap micro-programmed sequential FIR filter 10.56ns
16 bit Wallace tree multiplier [19]	4-tap micro-programmed sequential FIR filter 15.56ns	4-tap micro-programmed Parallel FIR filter 19.51ns
Virtex-4 (XC4VFX12) [17]	Serial FIR filter 24.648ns	Pipelined FIR filter 22.012ns
Virtex-5 (XC5VLX110T) [17]	Serial FIR filter 18.696ns	Pipelined FIR filter 15.928ns
Virtex-6 (XC6VCX75T) [17]	Serial FIR filter 17.411ns	Pipelined FIR filter 15.456ns
Proposed structure(Artix-7) (xc7a200tfbg676) (speed grade -1)	Par-pip FIR	
	5.124ns	

From Table 2, we can conclude that the proposed architecture is better than the existing structure since the delay is less hence, speed is improved in the combined pipelining and parallel processing architecture.

## 10. CONCLUSION

In this paper, we have implemented the combined pipelining and parallel processing architecture for both FIR and IIR filters. Synthesis and simulation are being carried out on Artix-7 series FPGA, target device (xc7a200tfg676) (speed grade -1) using VIVADO 2016.3. The parameters like area, delay and power are the main focus of this research work. With two stages of pipelining ( $M=2$ ) and three levels of parallelism ( $L=3$ ), FIR and IIR filters are being implemented and results are being analyzed and compared with the non-pipelined and non-parallel original filter. From the results, we observed that for FIR filter, in the combined architecture, with the decrease in area, power is reduced from 15.152W to 8.053W and delay also reduces from 9.347ns to 5.124ns. Ultimately, speed increased in the proposed combined architecture. For IIR filter, with a slight increase in the area in the combined architecture, power consumption is reduced from 10.375W to 5.293W at approximately equal speed. From Table 9.2, we can conclude that delay is less in this proposed architecture than the existing structures.

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