# ROBUST CONTENT BASED WATERMARKING ALGORITHM USING SINGULAR VALUE DECOMPOSITION OF RADIAL SYMMETRY MAPS

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#### ABSTRACT

Nowadays, image content is frequently subject to different malicious manipulations. To protect images from this illegal manipulations computer science community have recourse to watermarking techniques. To protect digital multimedia content we need just to embed an invisible watermark into images which facilitate the detection of different manipulations, duplication, illegitimate distributions of these images. In this work a robust watermarking technique is presented that embedding invisible watermarks into colour images the singular value decomposition bloc by bloc of a robust transform of images that is the Radial symmetry transform. Each bit of the watermark is inserted in a bloc of eight pixels large of the blue channel a high singular value of the corresponding bloc into the radial symmetry map. We justified the insertion in the blue channel by our feeble sensibility to perturbations in this colour channel of images. We present also results obtained with different tests. We had tested the imperceptibility of the mark using this approach and also its robustness face to several attacks.

#### **KEYWORDS**

Robust image watermarking, Invisible image watermarking, Radial symmetry maps, Singular value decomposition

### 1. Introduction

In recent decades, images are widely used, due to the progressive development of new imaging techniques and devices. Users of these techniques and devices share generally images over communication channels that can be unsecure. This wide transmission of image content make it easily modified and generally disregarding author's ownership that is gradually in danger because of these illegitimate manipulations. So the multimedia content protection became a rigorous need to defend the author's copyright and to protect multimedia content from different illegal manipulations.

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As a response to this need of protection come the digital watermarking of multimedia contents [1], [2]; which is no other than information hidden in the multimedia content such that a slight modification on the content results in a modification of the information hidden which is considered as a sign of unauthorized content's manipulation. A survey of watermarking techniques can be found in [3].

## 2. RELATED WORK

Our watermarking method belongs to the second generation approaches. In such approaches image content is used in digital watermarking throw the insertion of the mark in specific points of image like points of interest, edges, corners or other features [4]. A feature-based watermarking scheme was first proposed in [5] where the authors use the Mexican Hat wavelet scale interaction to extract features in the image that can resist a series of attacks which makes them suitable to be used as emplacement to insert and to extract the mark. Another content-based approach in [6] uses a reworked copy of the traditional Harris corner detector. The reworked copy calculates the corner response function within a circular window originate from the image centre and covers the largest area of it to resist image centre based rotation attacks. The new detector gives geometrically significant points that can detect possible geometric attacks. We find in [7] the use of interest points from the Harris corner detector to watermark synchronization before the extraction to recover the watermark positions that can be changed during a geometrical attack. To do, authors generate points of interest using the Harris detector after scale normalization in order to get the most stable points in the image by avoiding the sensitive character of the Harris detector face to scale changes. Then they search within a circular region around the detected points whether the detector response of a selected point reaches a local maximum or not. If it is the case they consider the point, otherwise they neglect it. After that they profit from the characteristic of Pseudo Zernike Moments magnitude which is invariant to rotation to design the watermark to embed in a rotation invariant pattern.

Another work [8] uses the robustness of interest's points to select the positions of the insertion which strengthen the relationship between the watermark and the image content. The detection of interest's points makes possible the creation of triangular partitions of the image and afterward the insertion of the watermark in each triangle. We note that image content is also used in watermarking systems in order to resist other geometric attacks like scale changing and translation in [9].

The watermarking scheme proposed in this paper uses image content through singular value decomposition (SVD). The use of SVD in watermarking schemes is not recent; we find in literature many watermarking schemes based on SVD decomposition [10], [11]. The SVD decomposition may be used in spatial or frequency domain. In frequency domain, the SVD decomposition can be combined with lifting wavelet transform like in [12]; it is also possible to combine it with the discrete cosines transform (DCT) as in [13] or many other transformations. The contribution of this work is the use of an SVD decomposition of a strong content transform (radial symmetry map) to insert in the blue channel where the red and the green channels are just used to synchronize the detection of the watermark.

## 3. SCHEME OVERVIEW

# 3.1. Imperceptibility and Robustness

A watermark can be visible or invisible, robust or fragile however in authors ownership protection applications a good watermarking algorithm is the one which is invisible and robust to different attacks. So in our proposed algorithm we take into account these two metrics to achieve a successful algorithm for the author copyright protection applications. To be invisible to human visual eye, first, the mark is inserted in the blue channel, which is the one to which the human visual system is less sensitive [14]. Second, the watermark bits are inserted in points of high interest in the image; those points with high luminance values make the modifications in the image imperceptible. That is the property of imperceptibility which mast marks any consistent watermarking scheme; the other property is the robustness of the system [15]. The robustness of our scheme is achieved by using robust transform of image information. This transform is called radial symmetry transform and it presents very good robustness against image transformations and nosing. The radial symmetry transform is originally used to detect image features [16], [17] and we use it in this work to support the robustness of the scheme and to detect pixels which care the mark bits.

## 3.2. Radial Symmetry Maps

Radial symmetry maps are generally used to detect interest points in images which correspond to object's centres. We find in literature many works on radial symmetry maps but the most commonly used is the one of [18]. Author in [18] details an algorithm to calculate the radial symmetry map of an image. With this approach a symmetry score is calculated from votes of one pixel to surrounding pixels. The transform is calculated in one or more radii n. the value of the transform at radius n indicates the contribution to radial symmetry of the gradients a distance n away from each point.

At each radius n, an orientation projection image  $O_n$  and a magnitude projection image  $M_n$  are formed. These images are generated by examining the gradient g at each point p from which a corresponding positively-affected pixel  $p_{+ve}(p)$  and negatively-affected pixel  $p_{-ve}(p)$  are determined, as shown in Figure 1. The positively-affected pixel is defined as the pixel that the gradient vector g (p) is pointing to, a distance n away from p, and the negatively-affected pixel is the pixel a distance n away that the gradient is pointing directly away from.

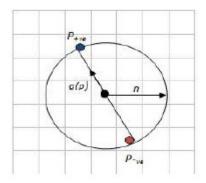


Figure 1. Positively and negativelly affected pixels

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Coordinates of the positively-affected pixel are given by:

$$p_{+ve} = p + ROUND \left( n \cdot \frac{g(p)}{\|g(p)\|} \right)$$
 (1)

Coordinates of the negatively-affected pixel are given by:

$$p_{-ve} = p - ROUND \left( n \cdot \frac{g(p)}{\|g(p)\|} \right)$$
(2)

The orientation and magnitude projection images are initially zero. For each pair of affected pixels, the corresponding point  $p_{+ve}$  in the orientation projection image  $O_n$  and magnitude projection image  $M_n$  is incremented by 1 and  $\|g(p)\|$ , respectively, while the point corresponding to  $p_{-ve}$  is decremented by these same quantities in each projection image. That is:

$$O_n(p_{+ve}(p)) = O_n(p_{+ve}(p)) + 1$$
 (3)

$$O_n(p_{-ve}(p)) = O_n(p_{-ve}(p)) - 1$$
 (4)

$$M_n(p_{+ve}(p)) = M_n(p_{+ve}(p)) + ||g(p)||$$
 (5)

$$M_n(p_{-ve}(p)) = M_n(p_{-ve}(p)) - ||g(p)||$$
 (6)

The radial symmetry contribution at radius n is defined as the convolution:

Where:

$$S_n = F_n * A_n \tag{7}$$

$$F_n(p) = \frac{M_n(p)}{k_n} \left( \frac{\left| \widetilde{O}_n(p) \right|}{k_n} \right)^{\alpha}$$
 (8)

And

$$\widetilde{O}_{n}(p) = \begin{cases} O_{n}(p) & \text{if On < kn} \\ k_{n} & \text{else} \end{cases}$$
(9)

 $A_n$  is a two-dimensional Gaussian,  $\alpha$  is the radial strictness parameter, and  $k_n$  is a scaling factor that normalizes  $M_n$  and  $O_n$  across different radii.

The full map is defined as the average of the symmetry contributions over all the radii considered:

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$$S = \frac{1}{|N|} \sum_{n \in N} S_n \tag{10}$$

### 4. THE PROPOSED SCHEME

The proposed algorithm inserts the watermark bits into the blue channel of the image based on an SVD decomposition of this channel. The SVD decomposition used here is a bloc based one which necessitates the decomposition of the blue channel into blocs of 8 pixels large in different locations in the image. The locations are objects centres obtained after a local maxima search over the radial symmetry map.

At the same time we should calculate the radial symmetry map using the red and green channel of the original image. The symmetry map is also divided into blocks of 8 pixels large in the same locations as the blue channel.

#### 4.1. Insertion of the watermark

To insert the pixel of the binary mark we need to calculate the svd of both, the blue block i and the symmetry transform map of the block i as indicated in Figure 2.

The insertion mechanism uses the formula:

$$\sigma_{bk} = W_i * \sigma_{sk} * \alpha \tag{11}$$

Where k is the index of the singular value which holds the mark.

 $\alpha$  is the embedding strength (an adjustment parameter between the quality and the robustness). It is chosen experimentally.

 $\sigma_{bk}$ ,  $\sigma_{sk}$  are respectively singular values from the range of big singular values of the blue bloc and those of the radial symmetry map bloc.

#### 4.2. Extraction of the watermark

Figure 3 presents the extraction scheme; it is based on the decomposition of blue image channel and radial symmetry map into blocs, then the decomposition of each bloc to its singular values.

To extract the watermark we use the singular values following the formula:

$$\widetilde{W}_{i} = \sigma_{blw} / \sigma_{slw} / \beta \qquad (12)$$

Where  $\beta$  is  $1/2\alpha$ ,  $\sigma_{bkw}$  and  $\sigma_{skw}$  are respectively singular values from high singular values of the blue blocs and those of the radial symmetry map of the watermarked image.

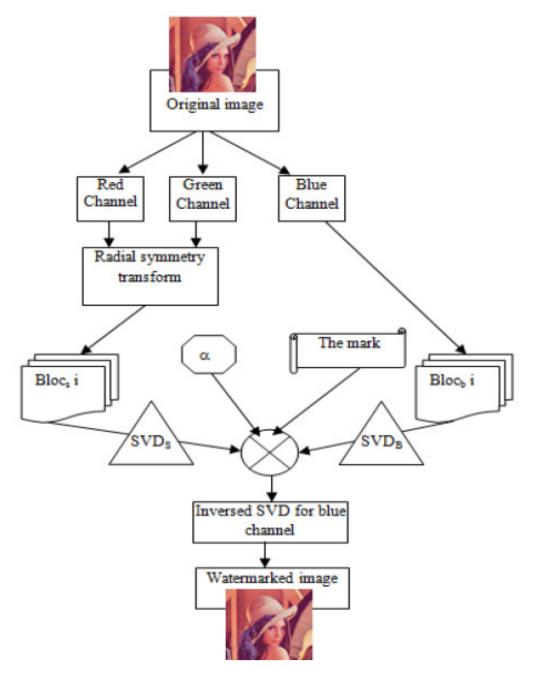


Figure 2. The mark insertion scheme

# 5. RESULTS AND DISCUSSION

This section presents tests results of imperceptibility and robustness for our scheme. We have tested our algorithm with and without attacks; table 1 presents the obtained results without attacks and table3 and table 4 present the results in presence of attacks. To test our watermarking scheme we use an image database composed of color images of size 512 x 512 pixels: Lena, baboon, air plane, peppers. The mark used is a binary image of size 8 x 8 pixels.

Figure 4 presents the original images used in tests with the watermark image to the right bottom of the figure.

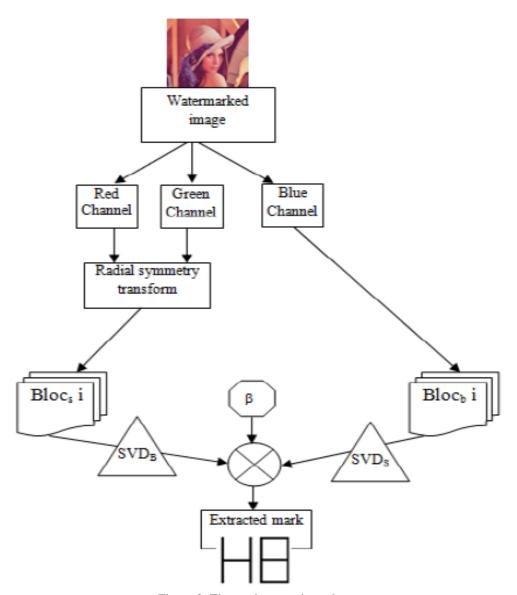


Figure 3. The mark extraction scheme

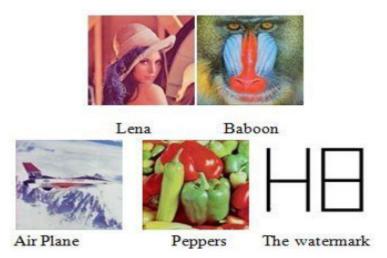


Figure 4. Test images with the watermark used

The table 1 presents the imperceptibility results according to tree objective measures: PSNR (Peak Signal to Noise Ratio) calculated between the original image and the watermarked one, NC (Normal Correlation) and BCR (Bit Correct Ratio) calculated between the original watermark and the extracted one.

We note that the results obtained with the PSNR measure between original image and the watermarked one are very good when we know that authors considered a PSNR rate as good when it is greater than 30dB. With tested images we have PSNR from 42 to 46dB.

When investigating table 1 we find that the NC measure is between 0.97 and 1 when the BCR measure is between 98.44% and 100%. These are very interesting rates which indicates that the proposed algorithm makes a high-quality extraction of the watermark.

To evaluate the robustness of our algorithm we should test its performance face to different attacks. The attack chosen are common in watermarking algorithm evaluation and includes low pass filtering, noise, jpeg compression and cropping. In this paper, we have used attacks with different parameters to check as deeply as possible the robustness of the proposed algorithm. Attacks used to test our watermarking system are given in table 2.

In this paper we have not tested the capacity of our proposed scheme, but we claim that our algorithm has a very good capacity since it inserts watermark bits into radial symmetry transform local maxima.

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Table 1. imperceptibility and robustness of the watermark in absence of attacks.

Image	PSNR	NC	BCR%		
Lena	+ 46.13 dB	1	100		
Baboon	+ 42.76 dB	0.97	98.44		
Air Plane	+ 45.42 dB	0.97	98.44		
Peppers	+ 45.42 dB	1	100		

Table 2. Attacks used in different tests.

	Attacks	Parameters			
SP1	Salt & Pepper noise	Density 0.008			
SP2	Salt & Pepper noise	Density 0.002			
SP3	Salt & Pepper noise	Density 0.05			
GN1	Gaussian noise	M=0.0 V=0.001			
GN2	Gaussian noise	M=0.1 V=0.001			
GF	Gaussian filter	3x3			
SH	Sharpening	3x3			
HE	Histogram equalization				
MF	Median filter	3x3			
JC1	JPEG Compression	Quality 80			
JC2	JPEG Compression	Quality 60			
CR	Cropping	1/8 of image			
AF	Average filter	3x3			
LF	Laplacian filter	3x3			
Rot1	Rotation	0.2°			

Table 3 presents the NC and BCR measure between the watermark inserted and the one extracted using our extraction scheme with different attacks over four test images.

By observing the interval of these two objective measures over all attacks (NC between 0.62 and 1, BCR between 71.88% and 100%) we can deduce that the proposed algorithm perform well face to these attacks. Furthermore, the robustness of the method is related to the tested image, thus to the content. Then, enhancing the content transform may enhance the extraction

The robustness of the algorithm face to the rotation attack can be reinforced using a robust rotational radial symmetry transform.

In the next figures (5-9) we present comparison graphics of NC rates between watermarks extracted with our algorithm and those presented in reference [12].

Algorithm in [12] uses gray scale images of 256 x 256 pixels where the watermark image is a binary image of 32 x 32 pixels which represents the letter "A". Table 4 summarises results of comparison of our algorithm and the algorithm of [12]. All algorithm [12] robustness values are extracted from reference [12].

N°	Lena		Baboon		Air	plane	Peppers		
	NC	BCR%	NC	BCR%	NC	BCR%	NC	BCR%	
SP1	0.88	89.06	0.97	98.44	1.00	100	1.00	100	
SP2	1.00	100	0.97	98.44	0.97	98.44	1.00	100	
SP3	0.73	71.88	0.90	78.13	0.90	79.69	0.73	75.00	
GN1	1.00	100	0.97	98.44	1.00	100	0.97	98.44	
GN2	1.00	100	0.97	96.88	0.97	98.44	0.97	98.44	
GF	1.00	100	0.97	98.44	0.97	98.44	1.00	100	
SH	1.00	93.75	0.97	98.44	1.00	100	0.97	98.44	
HE	1.00	100	0.97	98.44	0.91	95.31	0.84	92.19	
MF	0.90	95.31	0.82	90.63	0.77	87.50	0.71	82.81	
JC1	1.00	100	0.93	96.88	1.00	100	0.84	92.19	
JC2	0.81	90.63	0.73	87.50	0.94	96.88	0.63	81.25	
CR	0.93	95.31	0.98	98.44	0.93	95.31	1.00	100	
AF	0.85	92.19	0.73	84.38	0.66	79.69	0.62	78.13	
LF	0.71	85.94	0.90	95.31	0.90	95.31	0.80	90.63	
Rot1	0.90	93.31	0.84	92.19	0.85	92.19	0.81	90.63	

Table 3. Robustness of the proposed scheme (NC and BCR) over different attacks

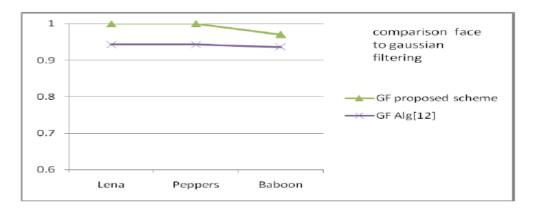


Figure 5. Comparaison of NC rates face to gaussian filtering

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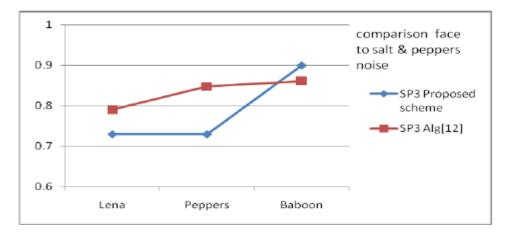


Figure 6. Comparaison of NC rates face to salt & peppers noise (density 0.05)

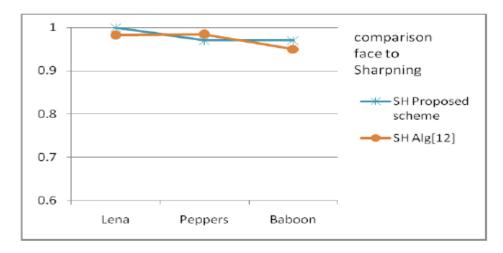


Figure 7. Comparaison of NC rates face to sharpening attack

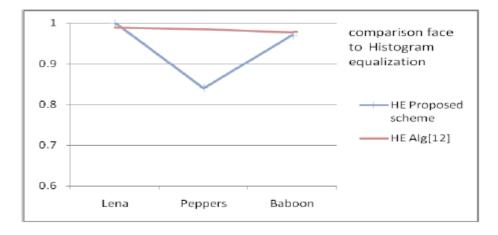


Figure 8. Comparaison NC rates face to histogram equalization attack



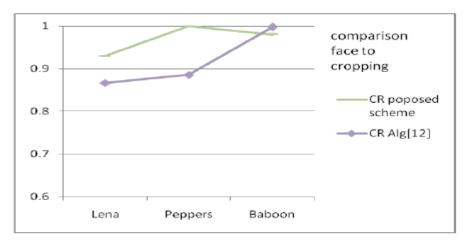


Figure 9. Comparaison of NC rates face to cropping attack

Table 4. Comparaison of the proposed algorithm with the algorithm of [12] in term of the two metrics NC and BCR

	Lena				Peppers				Baboon			
Attacks	Proposed scheme		Alg[12]		Proposed scheme		Alg[12]		Proposed scheme		Alg[12]	
N°	NC	BCR%	NC	BCR%	NC	BCR%	NC	BCR%	NC	BCR%	NC	BCR%
SP1	0.88	89.06	-	-	1.00	100	-	-	0.97	98.44	-	-
SP2	1.00	100	-	-	1.00	100	-	-	0.97	98.44	-	-
SP3	0.73	71.88	0.790	68.46	0.73	75.00	0.848	76.07	0.90	78.13	0.861	78.52
GN1	1.00	100	-	-	0.97	98.44	-	-	0.97	98.44	-	-
GN2	1.00	100	-	-	0.97	98.44	-	-	0.97	96.88	-	-
GF	1.00	100	0.943	90.63	1.00	100	0.943	90.72	0.97	98.44	0.936	89.65
SH	1.00	93.75	0.982	97.07	0.97	98.44	0.984	97.36	0.97	98.44	0.950	96.19
HE	1.00	100	0.988	98.05	0.84	92.19	0.984	97.36	0.97	98.44	0.977	96.19
MF	0.90	95.31	-	-	0.71	82.81	-	-	0.82	90.63	-	-
JC1	1.00	100	-	-	0.84	92.19	-	-	0.93	96.88	-	-
JC2	0.81	90.63	-	-	0.63	81.25	-	-	0.73	87.50	-	-
CR	0.93	95.31	0.867	79.10	1.00	100	0.886	82.23	0.98	98.44	0.998	99.61
AF	0.85	92.19	-	-	0.62	78.13	-	-	0.73	84.38	-	-
LF	0.71	85.94	-	-	0.80	90.63	-	-	0.90	95.31	-	-
Rot1	0.90	93.31	-	-	0.81	90.63	-	-	0.84	92.19	-	-

Figures (10-14) present comparison graphics of BCR rates between watermarks extracted with our algorithm and those presented in reference [12].

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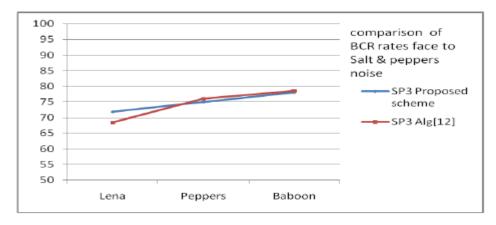


Figure 10. Comparaison of BCR rates face to salt & peppers noise (density 0.05)

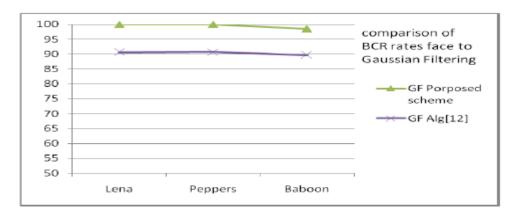


Figure 11. Comparaison of BCR rates face to gaussian filtering

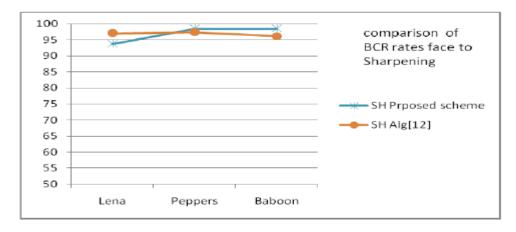


Figure 12. Comparaison of BCR rates face to sharpening attack

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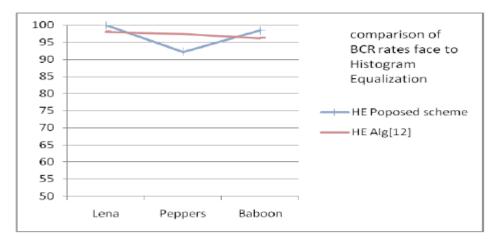


Figure 13. Comparaison BCR rates face to histogram equalization attack

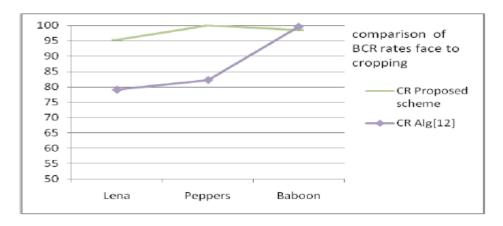


Figure 14. Comparaison of BCR rates face to cropping attack

### 6. CONCLUSION AND FURTHER WORKS

In this work, we present a new content based watermarking scheme which uses image content to improve robustness and two insure the correct extraction of the watermark in author ownership protection applications. The watermarking algorithm presented in this paper is a promised one since it presents good results in terms of robustness and imperceptibility. However, the approach necessitates to be compared to many other works in order to be judged correctly. To this date there are no works which evaluate different content based algorithms face to different attacks using unified metrics. So the comparison of this work with other works should be based on the same attacks and considering the same metrics. Since it is the case, we resolve, in our future work, to evaluate and to compare the present work with other content based watermarking techniques using a unified testing benchmark. We will work also on the enhancement of the radial symmetry maps so the points choosing to care the mark can be the most repetitive ones and the most robust to image manipulations.

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